



## NARASIMHA REDDY ENGINEERING COLLEGE

(Autonomous)

**Approved by AICTE, New Delhi & Affiliated to JNTUH, Hyderabad**

**Accredited by NAAC with A Grade, Accredited by NBA**

<b>Course Title</b>	:	Numerical Methods and Complex Variables
<b>Course Code</b>	:	23MA301
<b>Year &amp; Sem</b>	:	II – I
<b>Regulation</b>	:	NR23 (NRCM – NR23 Autonomous Syllabus)

### **QUESTION BANK**

#### **UNIT-I**

#### **LAPLACE TRANSFORMS**

S.No	Questions	BT	CO	Po
<b>Part – A (Short Answer Questions)</b>				
1	Find $L\{(sint+cost)^2\}$ .	L1,L 2	CO 1	Po1
2	Find $L\{(\sin 2t \cdot \cos 3t)\}$	L1,L 2	CO 1	Po1
3	Find $L\{\sqrt{t}e^{-3t}\}$	L1,L 2	CO 1	Po1
4	Define Laplace transform of a function f(t).	L1	CO 1	Po1
5	State First shifting theorem of Laplace transform	L1	CO 1	Po1
6	Find $L\left\{\frac{1-e^t}{t}\right\}$	L1,L 2	CO 1	Po1
7	Find $L^{-1}\left\{\frac{s^2-3s+4}{s^3}\right\}$	L1,L 2	CO 1	Po1
8	Find $L^{-1}\left\{\frac{1}{(s+1)^2}\right\}$	L1,L 2	CO 1	Po1
9	If $L\{f(t)\} = \frac{9s^2-12s+15}{(s-1)^3}$ , find $L\{f(3t)\}$ using change of scale property.	L1,L 2	CO 1	Po1
10	Find $L^{-1}\left\{\frac{1}{s(s+2)}\right\}$	L1,L 2	CO 1	Po1
<b>Part – B (Long Answer Questions)</b>				
11	a) Evaluate $L\{\int_0^t te^{-t} \sin 2t dt\}$ .	L3,L 5	CO 1	Po1
	b) Evaluate $L\left\{\frac{\cos \sqrt{t}}{\sqrt{t}}\right\}$	L3,L	CO	Po1

			5	1	
12	a)	Find $L\{te^{-t}\sin 2t \cos 2t\}$	L2	CO 1	Po1
	b)	Using Laplace transform, evaluate $\int_0^\infty \frac{\cos at - \cos bt}{t} dt$	L2	CO 1	Po1
13	a)	Find $L\{t^2 \cos 3t\}$	L2	CO 1	Po1
	b)	Find $L^{-1}\left\{\frac{s^2}{(s^2+4)(s^2+25)}\right\}$	L2	CO 1	Po1
14	a)	Using the Convolution theorem, find $L^{-1}\left\{\frac{s}{(s^2+a^2)^2}\right\}$	L3	CO 1	Po2
	b)	Find the inverse Laplace transform of $\left\{\frac{s+3}{(s^2+6s+13)^2}\right\}$	L2	CO 1	Po1
15		Solve the differential equation $\frac{d^2x}{dt^2} + 9x = \sin t$ using laplace transform given that $x(0)=1, x'(0)=0$	L5	CO 1	Po2
16		Using Laplace transform, evaluate $(D^2 + 5D + 6)x = 5e^t$ given that $x(0)=2, x'(0)=1$	L3	CO 1	Po2

**UNIT-II**  
**NUMERICAL METHODS-1**

S.No	Questions		BT	CO	PO												
<b>Part – A (Short Answer Questions)</b>																	
1	Write the merits and demerits of the Newton Raphson method.	L1	CO2	Po1													
2	Write the merits and demerits of the Regula-falsi method.	L1	CO2	Po1													
3	Show that $\mu = \frac{1}{2}(E^{\frac{1}{2}} + E^{-\frac{1}{2}})$ .	L2	CO2	Po1													
4	Prove that $\nabla = 1 - E^{-1}$ .	L1	CO2	Po1													
5	Evaluate $\Delta^2 e^{2x+3}$ .	L1	CO2	Po1													
6	Show that $\Delta f_i^2 = (f_i + f_{i+1})\Delta f_i$ .	L1	CO2	Po1													
7	Define Newton Forward Interpolation formula.	L1	CO2	Po1													
8	Define Newton Backward Interpolation formula.	L1	CO2	Po1													
9	State Lagrange's Interpolation formula.	L1	CO2	Po1													
10	Evaluate $\sqrt{28}$ to four decimal places by newton's iterative method	L2	CO2	Po2													
<b>Part – B (Long Answer Questions)</b>																	
11	a)	Find the real root for $x \tan x + 1 = 0$ using newton Raphson method	L3	CO2	Po1												
	b)	find the real root of the equation $x e^x = \cos x$ using the regula false method correct to four decimal places	L3	CO2	Po1												
12		consider the following data for $g(x) = \frac{\sin x}{x^2}$ calculate $g(0.25)$ accurately using newton's forward method of interpolation <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>0.1</td><td>0.2</td><td>0.3</td><td>0.4</td><td>0.5</td></tr> <tr> <td>g(x)</td><td>9.9833</td><td>4.9696</td><td>3.2836</td><td>2.4339</td><td>1.9177</td></tr> </table>	x	0.1	0.2	0.3	0.4	0.5	g(x)	9.9833	4.9696	3.2836	2.4339	1.9177	L2	CO2	Po1
x	0.1	0.2	0.3	0.4	0.5												
g(x)	9.9833	4.9696	3.2836	2.4339	1.9177												
13		Find $Y(66)$ given that $Y(50)=201, Y(60)=225, Y(70)=248$ and $Y(80)=274$ using newton's backward difference formula	L3	CO2	Po1												
		Using Lagrange's Interpolation formula find $y(10)$ from the following table <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>5</td><td>6</td><td>9</td><td>11</td></tr> <tr> <td>y</td><td>12</td><td>13</td><td>14</td><td>16</td></tr> </table>	x	5	6	9	11	y	12	13	14	16	L3	CO2	Po1		
x	5	6	9	11													
y	12	13	14	16													

14	a)	Find the real root of $x^3 - x - 2 = 0$ , using Newton Raphson method.	L2	CO2	Po1												
	b)	Find the positive root of the equation $f(x) = x^3 - 2x - 5 = 0$ , using Regula-falsi method.	L2	CO2	Po1												
15		From the following table estimate the number of students who obtained marks between 40 & 45, Using Newton Forward Interpolation <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>Marks</td><td>30-40</td><td>40-50</td><td>50-60</td><td>60-70</td><td>70-80</td></tr> <tr> <td>No. of students</td><td>31</td><td>42</td><td>51</td><td>35</td><td>31</td></tr> </table>	Marks	30-40	40-50	50-60	60-70	70-80	No. of students	31	42	51	35	31	L2	CO2	Po2
Marks	30-40	40-50	50-60	60-70	70-80												
No. of students	31	42	51	35	31												
16		Given $U_1=22, U_2=30, U_4=82, U_7=106, U_8=206$ find $U_6$ use Lagrange's interpolation formula.	L2	CO2	Po2												

**UNIT-III**  
**NAME NUMERICAL METHODS-II**

S.No	Questions			BT	CO	PO																
<b>Part – A (Short Answer Questions)</b>																						
1	Write the Simpson's 1/3 and 3/8 rule.			L1	CO3	Po1																
2	Evaluate $\int_1^2 e^{-\left(\frac{1}{2}\right)x} dx$ using trapezoidal rule given that <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>1</td><td>1.25</td><td>1.5</td><td>1.75</td><td>2</td></tr> <tr> <td>y</td><td>0.6065</td><td>0.5352</td><td>0.4724</td><td>0.4169</td><td>0.3679</td></tr> </table>			x	1	1.25	1.5	1.75	2	y	0.6065	0.5352	0.4724	0.4169	0.3679	L3	CO3	Po1				
x	1	1.25	1.5	1.75	2																	
y	0.6065	0.5352	0.4724	0.4169	0.3679																	
3	The table below show the temperature $f(t)$ as a function of time <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>t</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr> <tr> <td>f(t)</td><td>81</td><td>75</td><td>80</td><td>83</td><td>78</td><td>70</td><td>60</td></tr> </table> Evaluate $\int_1^7 f(t)dt$ using Simpson's 1/3 rule.			t	1	2	3	4	5	6	7	f(t)	81	75	80	83	78	70	60	L2	CO3	Po1
t	1	2	3	4	5	6	7															
f(t)	81	75	80	83	78	70	60															
4	Using Simpson's 3/8 rule estimate $\int_0^6 \frac{dx}{1+x^2}$ , by dividing the range into 6 equal parts			L2	CO3	Po1																
5	Estimate $\int_0^1 e^{-x^2} dx$ using Simpson's 1/3 rule taking $h=0.1$ .			L3	CO3	Po1																
6	Explain Picard's method.			L1	CO3	Po1																
7	Write the merits and demerits of Euler's method.			L1	CO3	Po1																
8	Write the Runge-kutta second order formulae.			L1	CO3	Po1																
9	Write the Runge-kutta fourth order formulae.			L1	CO3	Po1																
10	If $\frac{dy}{dx} = x + y, y(0) = 2$ , then find $y(0.1)$ by Euler's method.			L2	CO3	Po1																
<b>Part – B (Long Answer Questions)</b>																						
11	a)	Use the trapezoidal rule with $n=4$ to estimate $\int_0^1 \frac{dx}{1+x^2}$ , correct to four decimal places			L2	CO3	Po1															
	b)	Find the value of $\int_1^2 \frac{dx}{x}$ by simpson's 1/3 rule. Hence obtain approximate value of $\log_e 2$ .			L2	CO3	Po1															
12	a)	Evaluate $\int_0^1 x\sqrt{1+x^4} dx$ using simpson's 3/8 rule.			L3	CO3	Po1															
	b)	Find $y(0.1), y(0.2), Z(0.1), Z(0.2)$ given $\frac{dy}{dx} = x + z, \frac{dz}{dx} = x - y^2$ and $Y(0)=2, Z(0)=1$ by using taylor's series method.			L3	CO3	Po1															

13		Find the value of y at x=0.1 by picard's method, given that $\frac{dy}{dx} = \frac{y-x}{y+x}$ , $y(0) = 1$ .	L3	CO3	Po1
14	a)	Using Euler's method ,solve for y at x=2 from $\frac{dy}{dx} = 3x^2 + 1$ , $y(1)=2$ , taking step size (i) 0.5 (ii) 0.25	L3	CO3	Po1
	b)	Given $\frac{dy}{dx} = -xy^2$ , $Y(0)=2$ compute $Y(0.2)$ in steps of 0.1 using modified Euler's method	L3	CO3	Po1
15	a)	Given $y' = x-y$ , $y(0)=1$ ,compute $y(0.2)$ with $h=0.1$ using modified Euler's method	L3	CO3	Po1
	b)	Use Runge-kutta method to evaluate $Y(0.1)$ and $y(0.2)$ given that $y' = x+y$ , $y(0)=1$	L3	CO3	Po1
16	a)	Using Runge-kutta method of fourth order, solve $\frac{dy}{dx} = \frac{y^2-x^2}{y^2+x^2}$ with $y(0) = 1$ at $x=0.2,0.4$ .	L3	CO3	Po1
	b)				

**UNIT-IV**  
**COMPLEX VARIABLE (DIFFERENTIATION)**

S.No	Questions			BT	CO	PO
<b>Part – A (Short Answer Questions)</b>						
1	Find all values of k such that $f(z)=e^x(\cos ky + i\sin ky)$ is analytic.	L1	CO4	Po1		
2	Show that $z^2$ is analytic for all z.	L1	CO4	Po1		
3	Show that the function $f(z)=\sin x \cosh y + i \cos x \sinh y$ is continuous as well as analytic everywhere.	L1	CO4	Po1		
4	Define Cauchy-Reimann equations in polar form.	L1	CO4	Po1		
5	Define harmonic function.	L1	CO4	Po1		
6	Define analytic function.	L1	CO4	Po1		
7	Separate the real and imaginary parts of $\cot z$ .	L1	CO4	Po1		
8	Find the real and imaginary parts of $e^{z^2}$	L1	CO4	Po1		
9	Prove that $\overline{\sin z} = \sin \bar{z}$	L1	CO4	Po1		
10	Find all the roots of the equation $\sin z=2$ .	L2	CO4	Po1		
<b>Part – B (Long Answer Questions)</b>						
11	a)	State Cauchy-Riemann equation and if $f(z)$ is a regular function of z, prove that $\left[ \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right]  f(z) ^2 = 4 f'(z) ^2$	L2	CO4	Po1	
	b)	If $\tan(\log(x+iy)) = a+ib$ , where $a^2+b^2 \neq 1$ show that $\frac{2a}{1-a^2-b^2} =$	L3	CO4	Po	

		Tan(log(x <sup>2</sup> + y <sup>2</sup> )).			1
12	a)	Define analytic function and show that both the real and imaginary parts of an analytic function satisfied Laplace's equation (are harmonic).	L2	CO4	Po 1
	b)	Define polar form of Cauchy-Riemann equation and prove that Z <sup>n</sup> is analytic and hence find its derivative.	L2	CO4	Po 1
13		Prove that the function f(z) defined by $f(z)=\begin{cases} \frac{x^3(1+i)-y^3(1-i)}{x^2+y^2}, & z \neq 0 \\ 0, & z = 0 \end{cases}$ is continuous and the Cauchy-Riemann equation are satisfied at the origin ,yet f'(0) does not exist .	L2	CO4	Po 1
14	a)	If Tan(x+iy)= A+ iB, then prove that A <sup>2</sup> +B <sup>2</sup> -2Bcoth2y+1=0	L3	CO4	Po 1
	b)	Find k such that f(x,y)=x <sup>3</sup> +3kxy <sup>2</sup> may be harmonic and find its conjugate.	L3	CO4	Po 1
15	a)	separate the real and imaginary parts of (i) cotz (ii) tanhz.	L2	CO4	Po 1
	b)	Show that u(x,y) = e <sup>2x</sup> (x cos2y - y sin2y) is harmonic and find its harmonic conjugate.	L3	CO4	Po 2
16	a)	Prove that $u = e^{-x}[(x^2 - y^2)cosy + 2xysiny]$ is harmonic and find the analytic function whose real part is u	L3	CO4	Po 1
	b)	Find the ayalytic function whose imaginary part is $\frac{2sinxsiny}{cos2x+cosh2y}$	L3	CO4	Po 1

**UNIT-V**  
**COMPLEX VARIABLE (INTEGRATION )**

S.No	Questions		BT	CO	PO
<b>Part – A (Short Answer Questions)</b>					
1	Evaluate $\int_0^{1+i} (x - y^2 + ix^3) dz$ along the real axis from z=0 to z=1.	L2	CO5	Po1	
2	Evaluate $\int_C \frac{z^2-z+1}{z-1} dz$ where C:  z  = 1/2.	L3	CO5	Po1	
3	State Cauchy's Integral theorem.	L1	CO5	Po1	
4	Evaluate $\int_C \frac{e^z}{(z+1)^2} dz$ around C:  z - 1  = 3.	L3	CO5	Po1	
5	Evaluate $\int_1^3 (Z - 2)^3 dz$	L1	CO5	Po1	
6	State Taylor's theorem.	L1	CO5	Po1	
7	State Laurent's theorem.	L1	CO5	Po1	
8	State Cauchy's Residue theorem.	L1	CO5	Po1	
9	Determine the pole of the function cotz.	L1	CO5	Po1	
10	Find the residue of $\frac{ze^z}{(z-1)^3}$ at its pole.	L2	CO5	Po1	
<b>Part – B (Long Answer Questions)</b>					
11	a)	Evaluate $\int_C (y^2 + 2xy)dx + (x^2 - 2xy)dy$ where c is the boundary of the region by y=x <sup>2</sup> and x=y <sup>2</sup> .	L3	CO5	Po1
	b)	State Cauchy's theorem and verify Cauchy's theorem for the function f(z)=	L3	CO5	Po1

		3z <sup>2</sup> +iz-4 if c is the square with vertices at 1±i and -1 ± i.			
12	a)	Evaluate $\int_c \frac{\log z}{(z-1)^3} dz$ where c:  z - 1 =1/2 using cauchy's integral formula.	L3	CO5	Po1
	b)	Using Cauchy's integral formula, evaluate $\int_c \frac{z^4}{((z+1)(z-i)^2} dz$ where c is the ellipse $9x^2 + 4y^2=36$ .	L3	CO5	Po1
13	a)	Evaluate $\int_c \frac{z^3 - \sin 3z}{(z-\frac{\pi}{2})^3} dz$ with c: z =2 using cauchy's integral formula.	L5	CO5	Po1
	b)	Find the Laurent series expansion of the function $f(z)=\frac{z^2-6z-1}{(z-1)(z-3)(z+2)}$ in the region $3< z+2 <5$ .	L3	CO5	Po2
14	a)	Obtain the Taylor's series to represent the function $\frac{z^2-1}{(z+2)(z+3)}$ in the region $ z  < 2$ .	L2	CO5	Po1
	b)	Evaluate $\oint_c \frac{4-3z}{z(z-1)(z-2)} dz$ where c is the circle $ z  = \frac{3}{2}$ using residue theorem.	L3	CO5	Po2
15		Show that $\int_0^{2\pi} \frac{1}{2+\cos\theta} d\theta = \frac{2\pi}{\sqrt{3}}$ .	L3	CO5	Po1
16		Evaluate $\int_{-\infty}^{\infty} \frac{x^2}{(x^2+1)(x^2+4)} dx$ using residue theorem.	L3	CO5	Po2

\* **Blooms Taxonomy Level (BT)** (L1 – Remembering; L2 – Understanding; L3 – Applying; L4 – Analyzing; L5 – Evaluating; L6 – Creating)

**Course Instructor**

**Head of the Dept.**