

## **MODULE-II**

### **SYMMETRIC KEY CIPHER**

- Block Cipher principles, DES, AES, Blowfish, RC5, IDEA, Block cipher operation, Stream ciphers, RC4.

### **ASYMMETRIC KEY CIPHERS**

- Principles of public key cryptosystems, RSA algorithm, Elgamal Cryptography, Diffie-Hellman Key Exchange, Knapsack Algorithm.

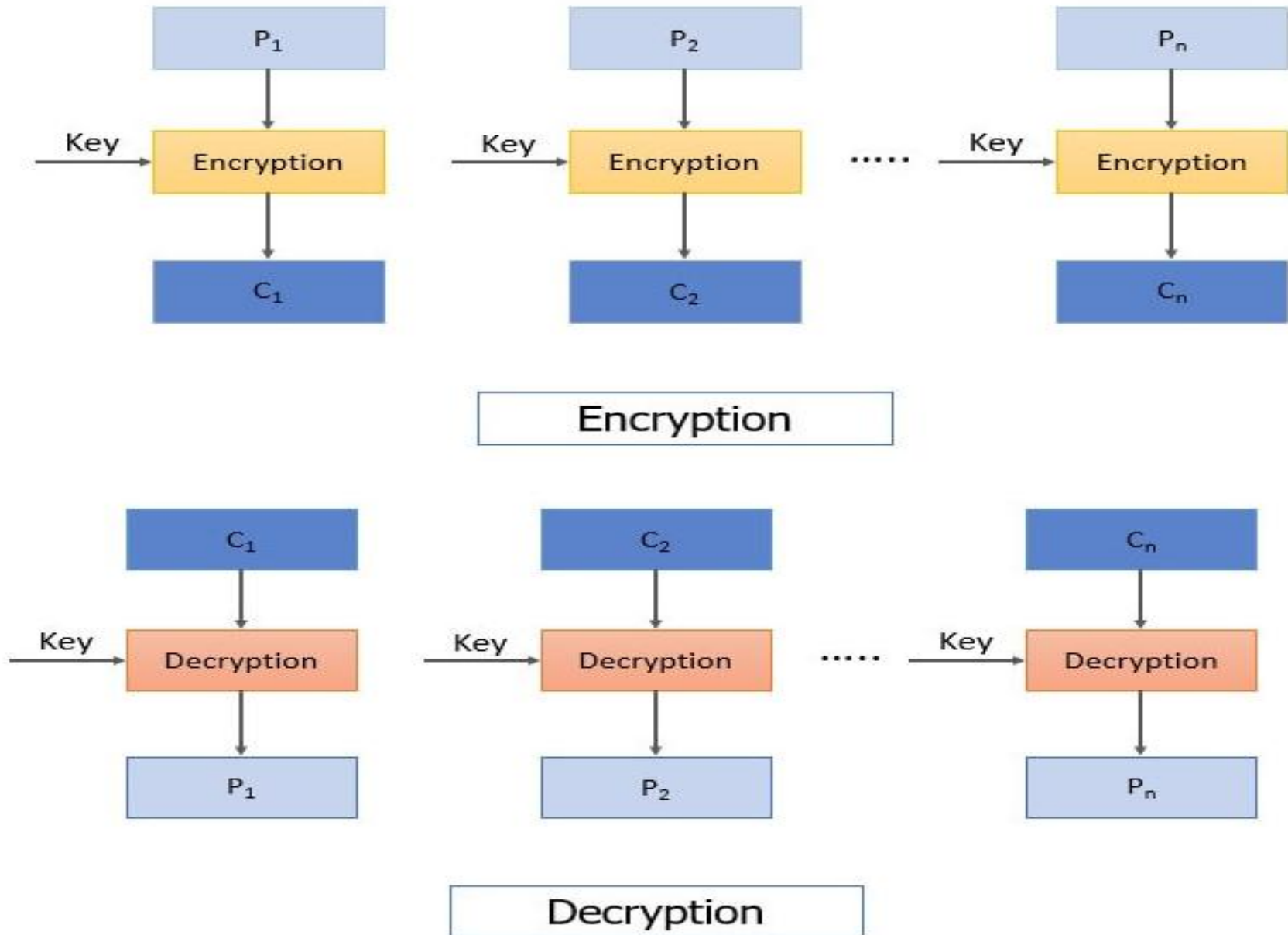
# Block Cipher principles

- Block cipher is an encryption method which divides the plain text into blocks of fixed size. Each block has an equal number of bits. At a time, block cipher operates only on one block of plain text and applies key on it to produce the corresponding block of ciphertext.
- **Block Cipher Principles**
  - Number of Rounds
  - Design of Function F
  - Key Schedule Algorithm

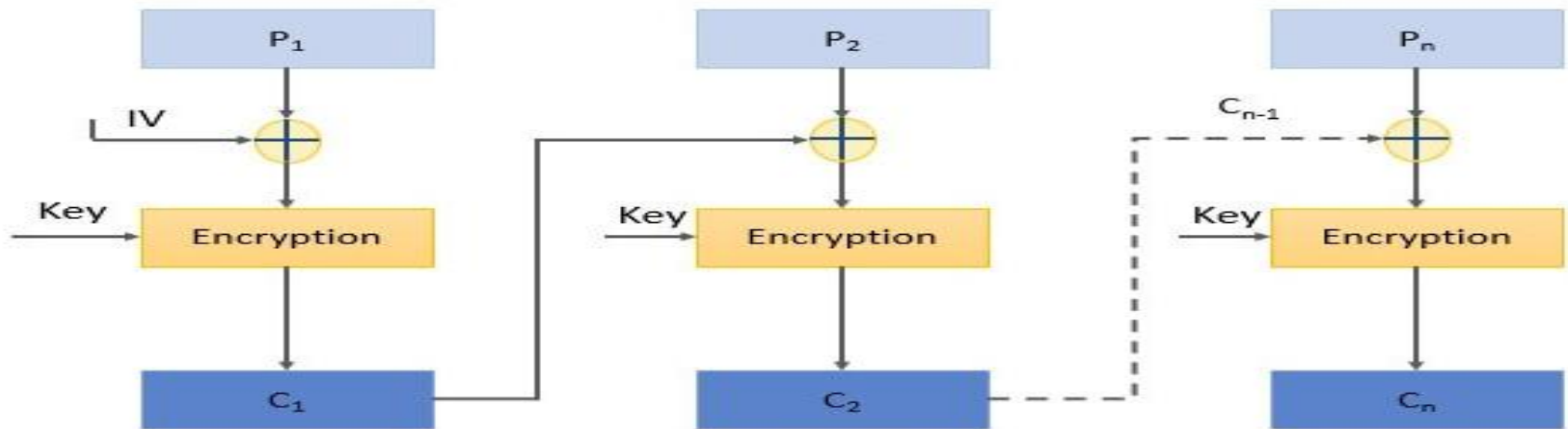
# Cipher Block modes of Operation

- **Electronic Code Book (ECB)**
- **Cipher Block Chaining Mode (CBC)**
- **Cipher Feed Back Mode (CFB)**
- **Output Feedback Mode (OFB)**
- **Counter Mode (CTR)**

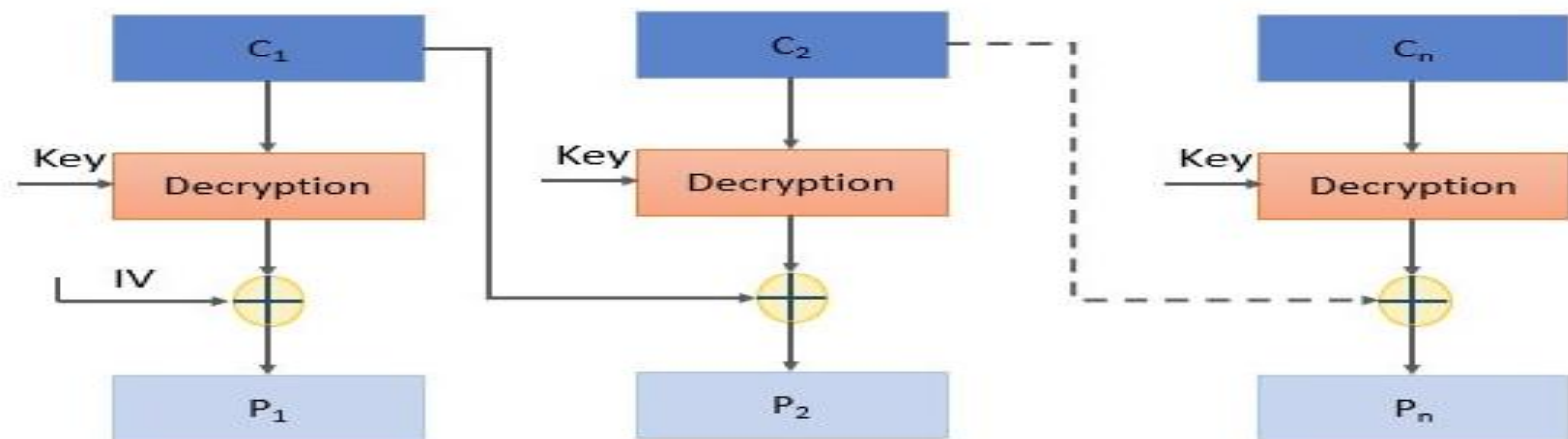
# Electronic Code Book (ECB)



# Cipher Block Chaining Mode (CBC)

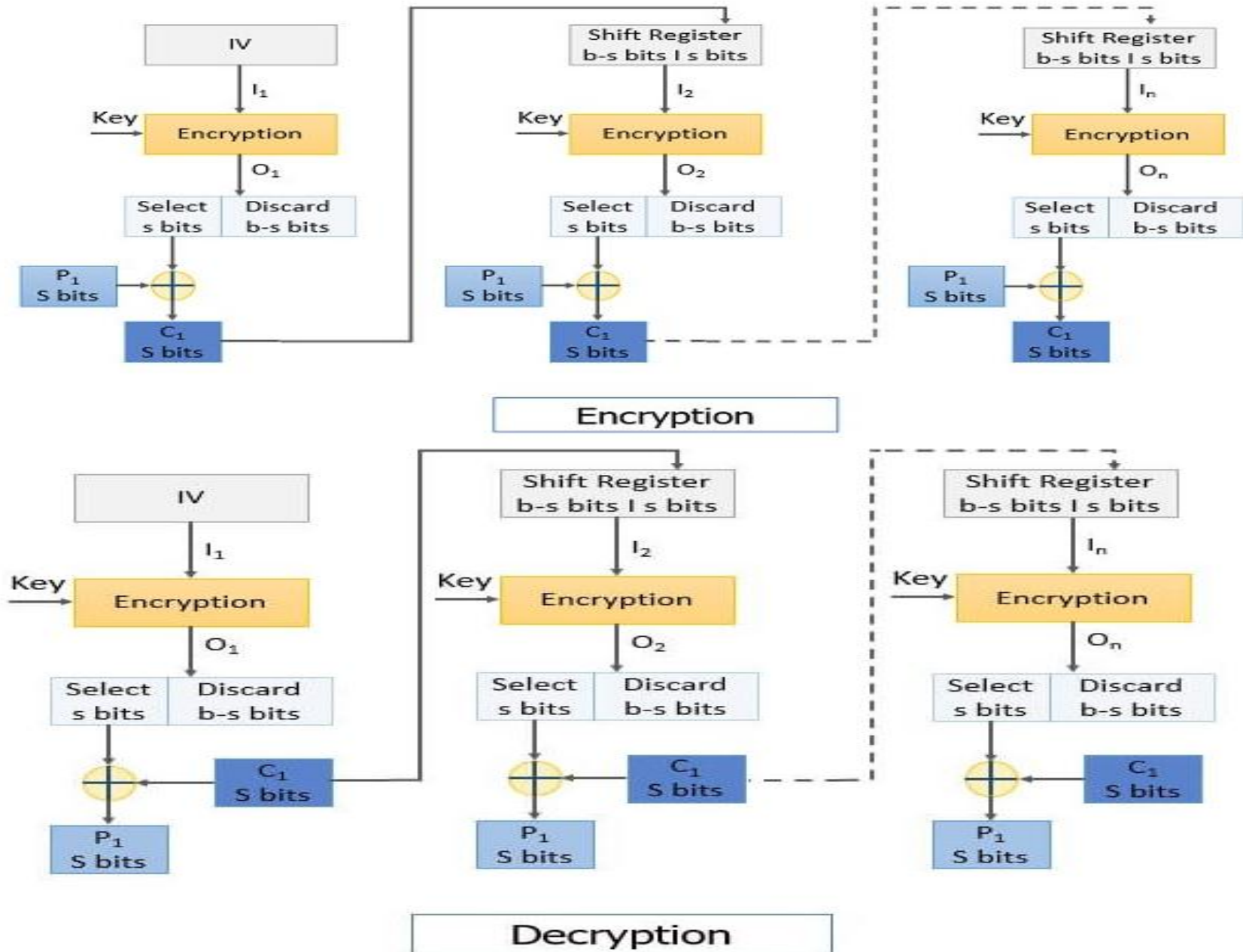


Encryption

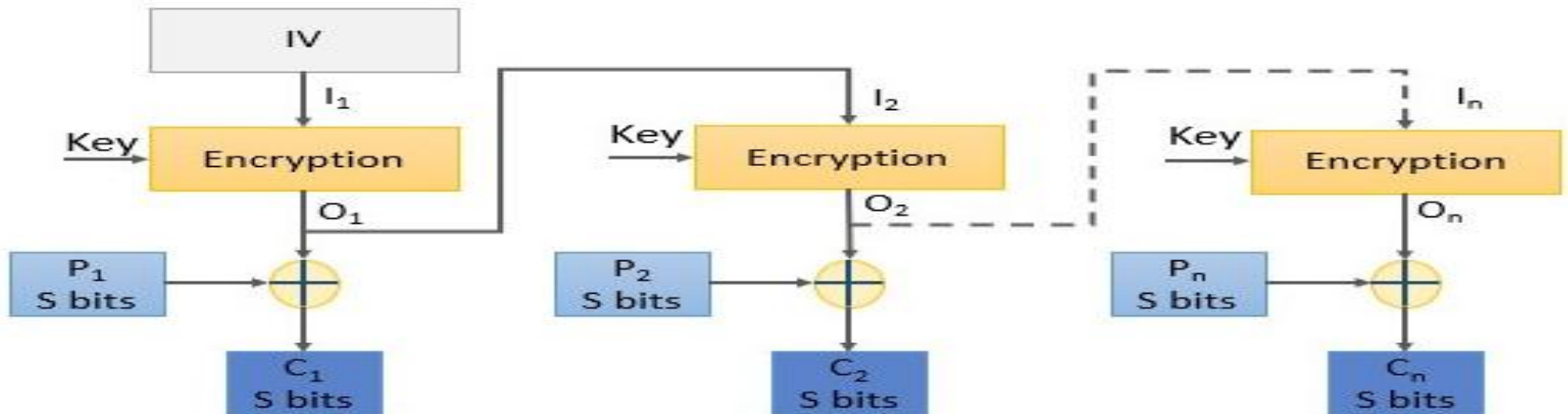


Decryption

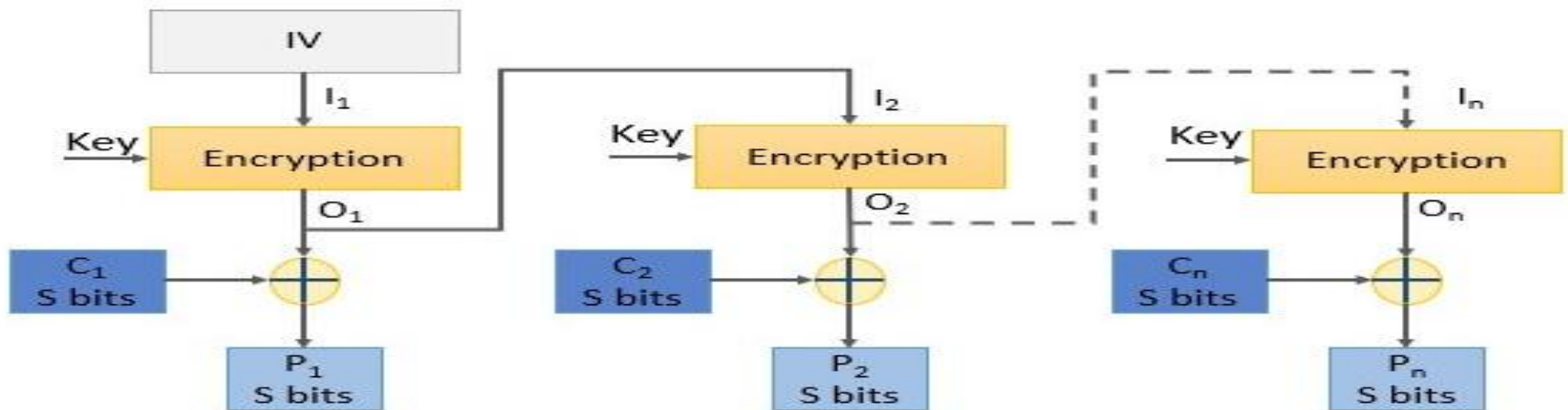
# Cipher Feed Back Mode (CFB)



# Output Feedback Mode (OFB)

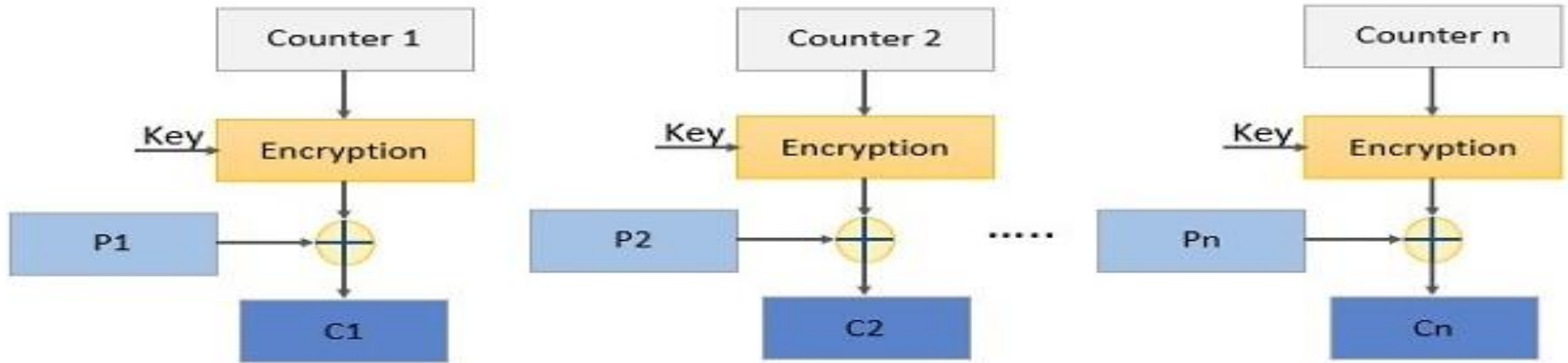


Encryption

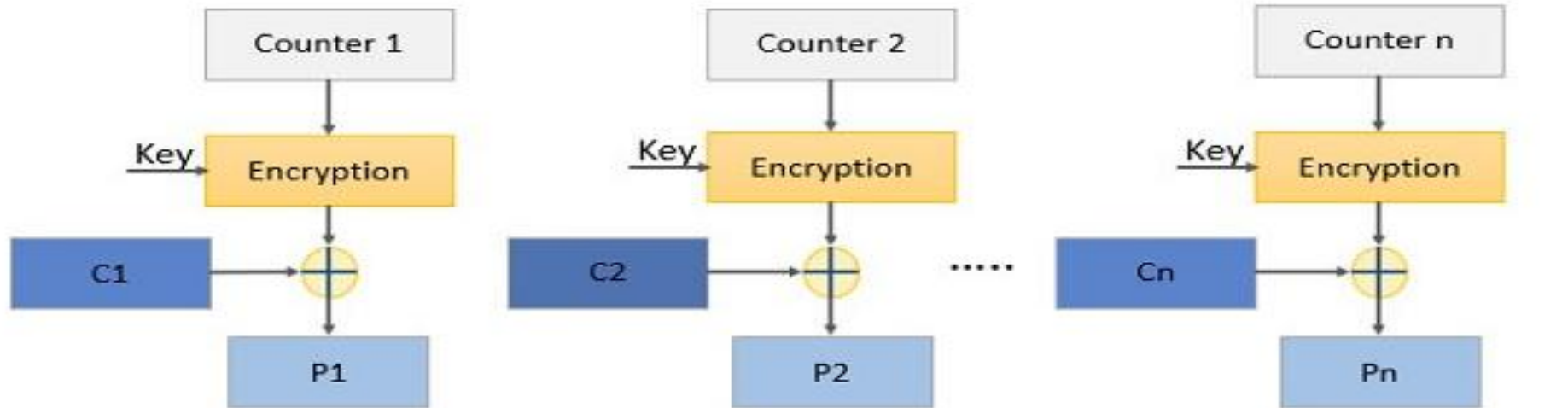


Decryption

# Counter Mode (CTR)

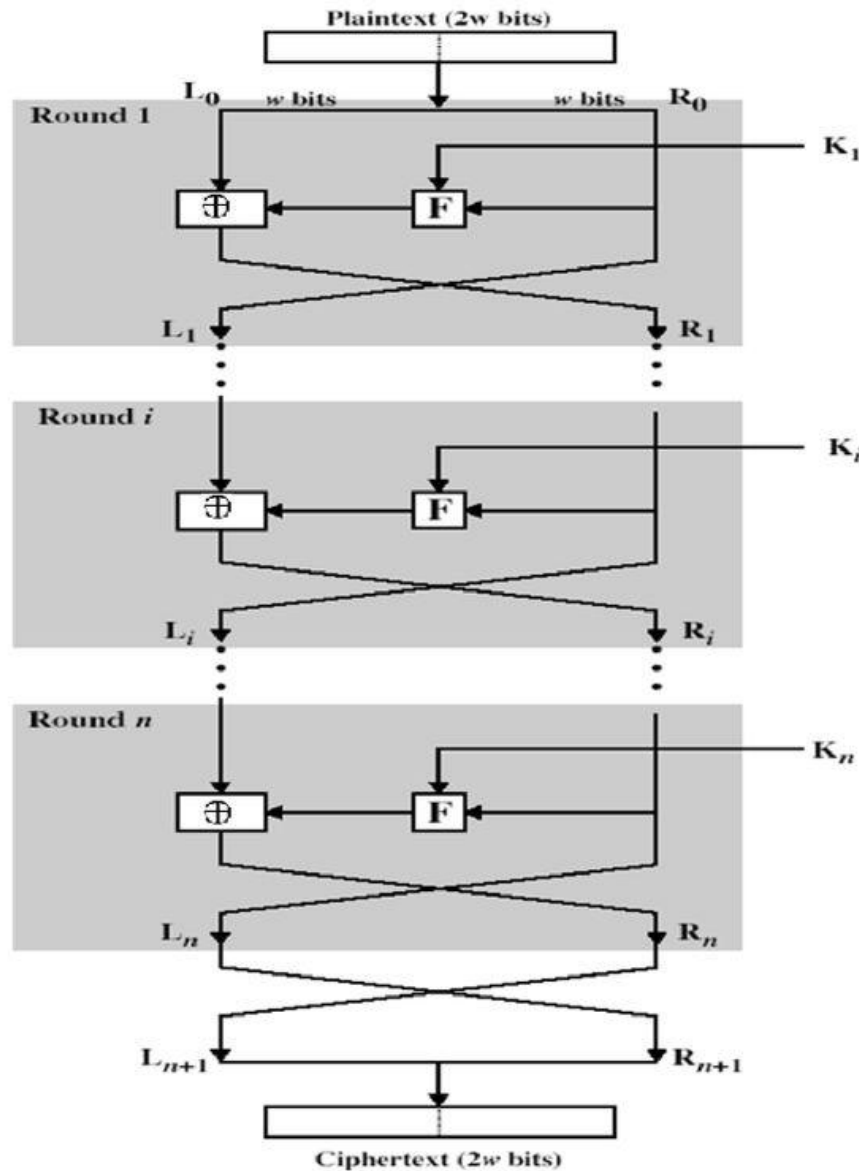


Encryption

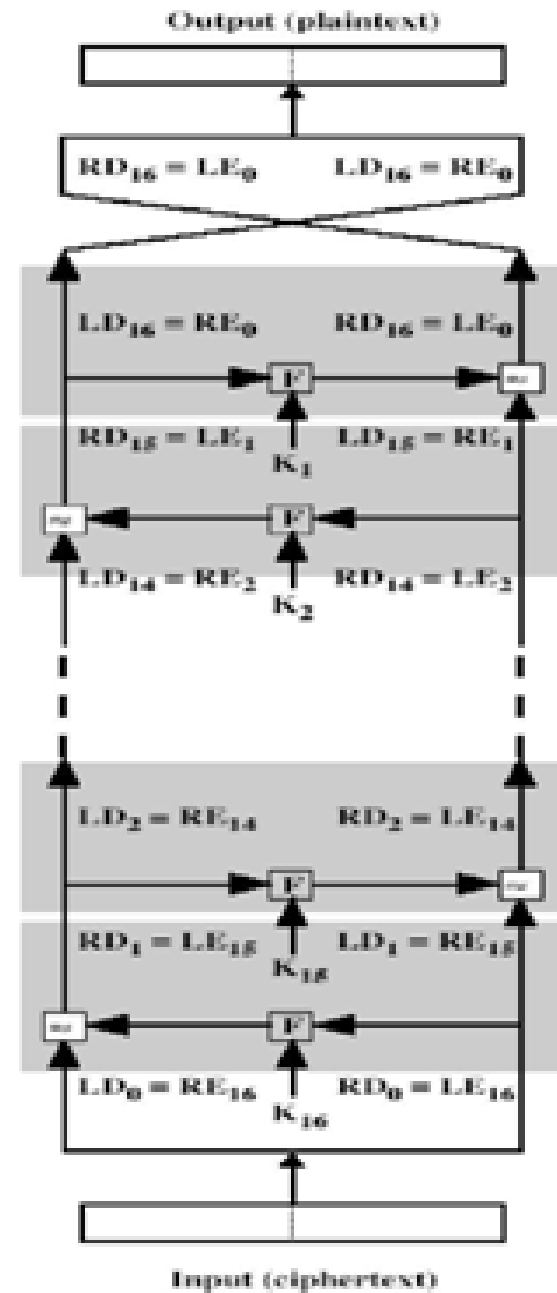
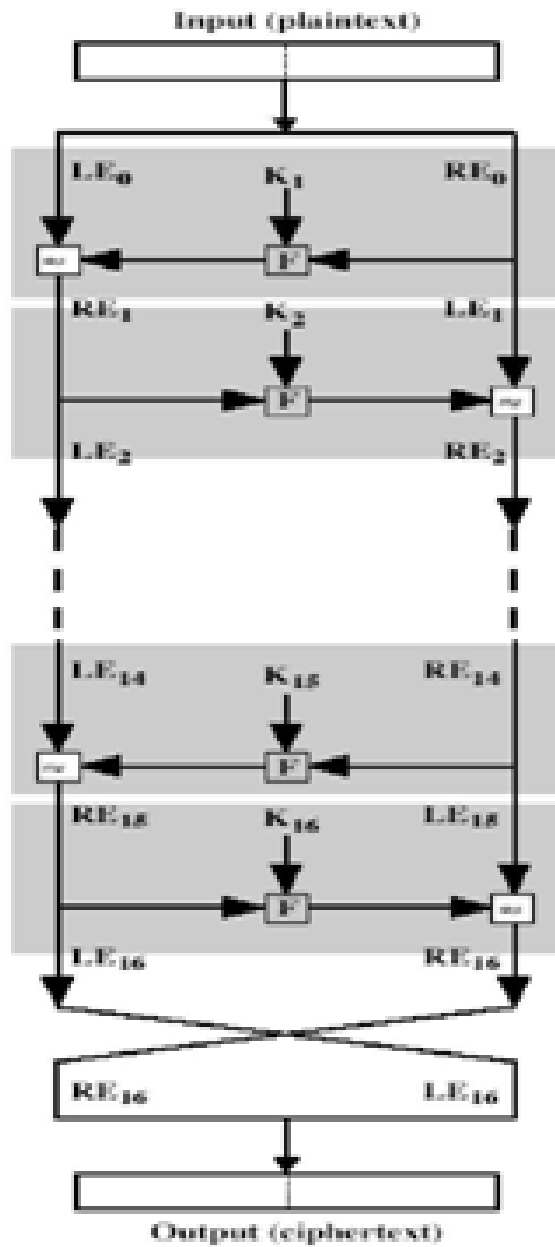


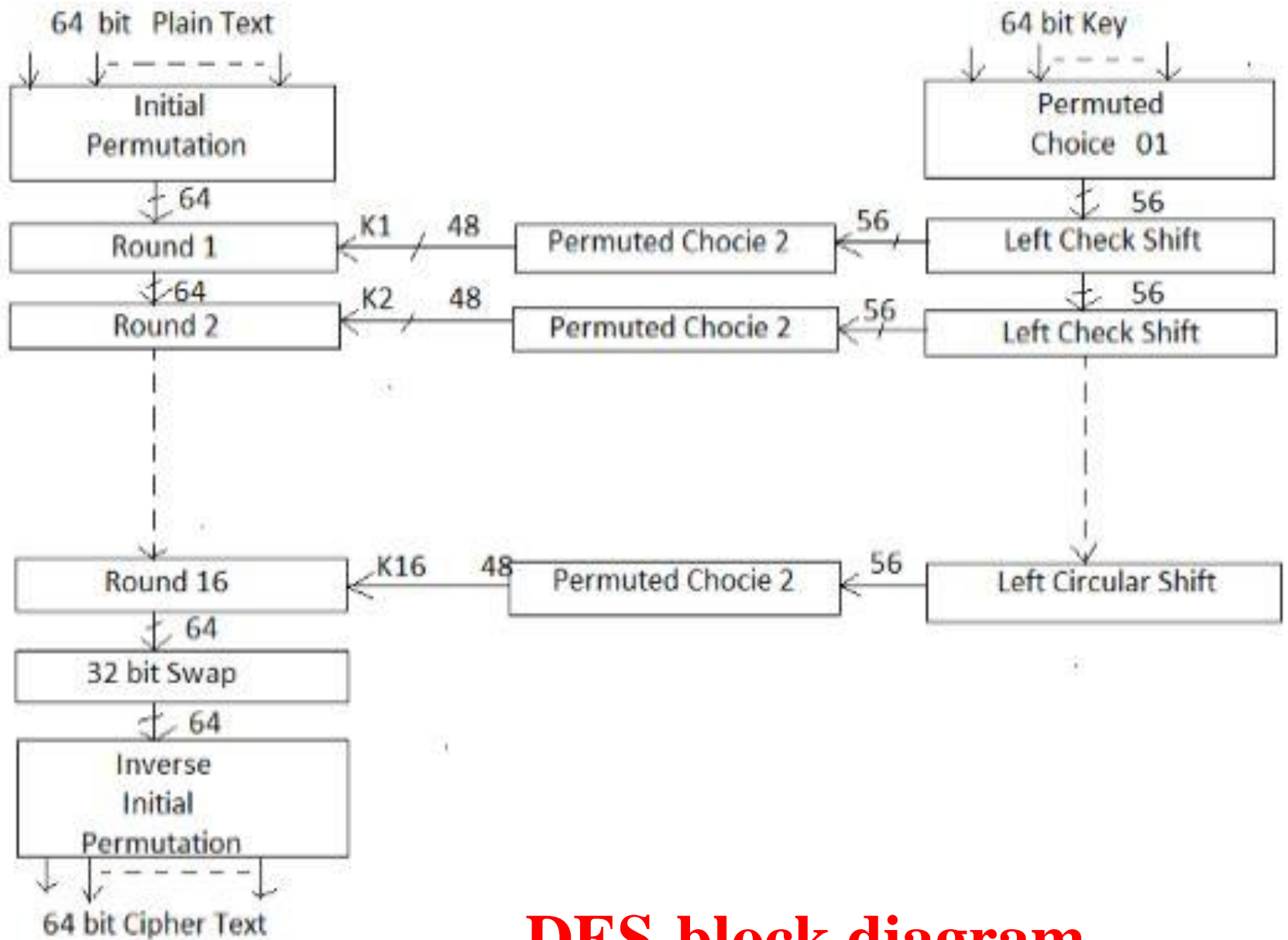
Decryption

# Feistel Cipher Structure

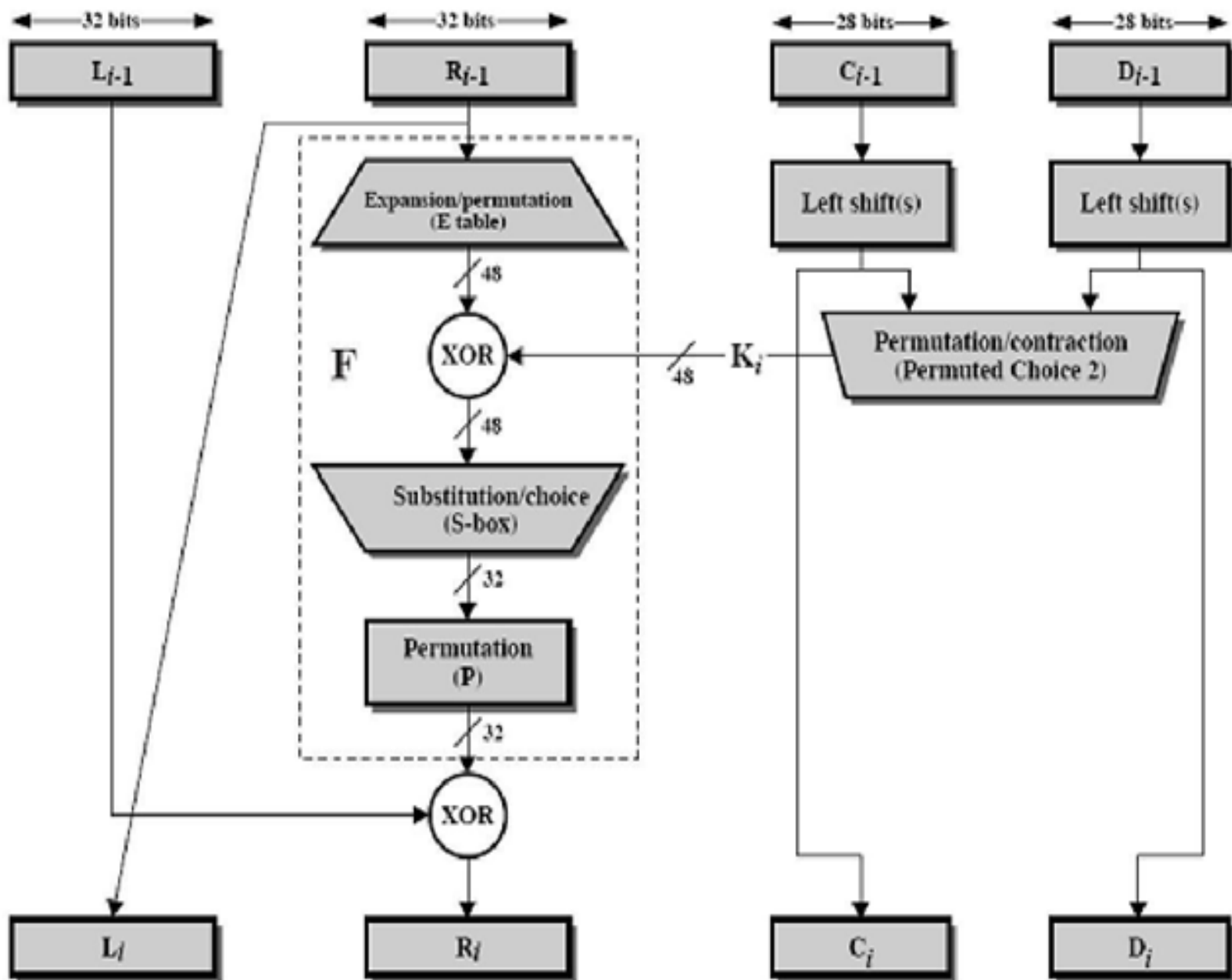


Feistel  
Cipher  
Structure





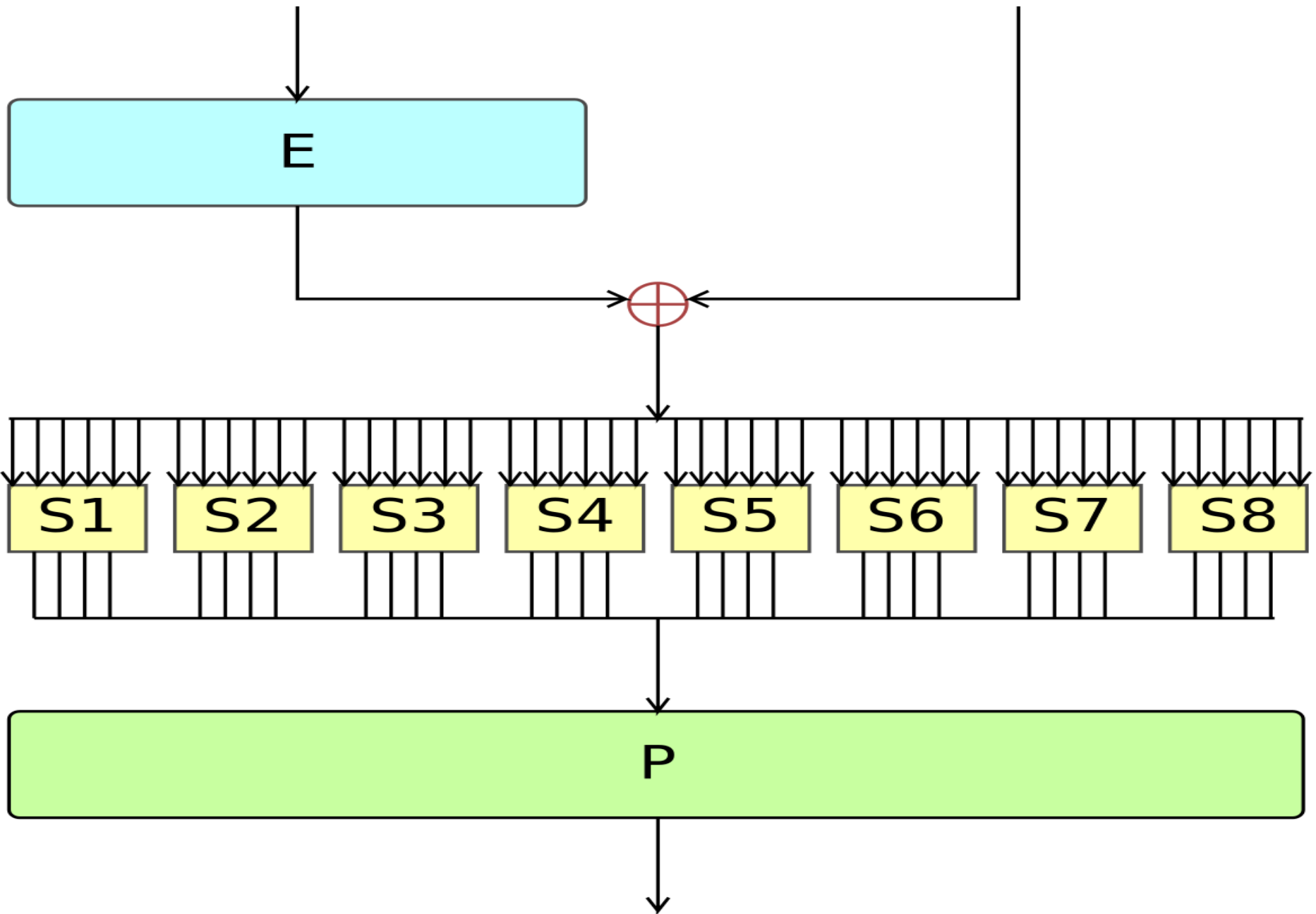
**DES-block diagram**

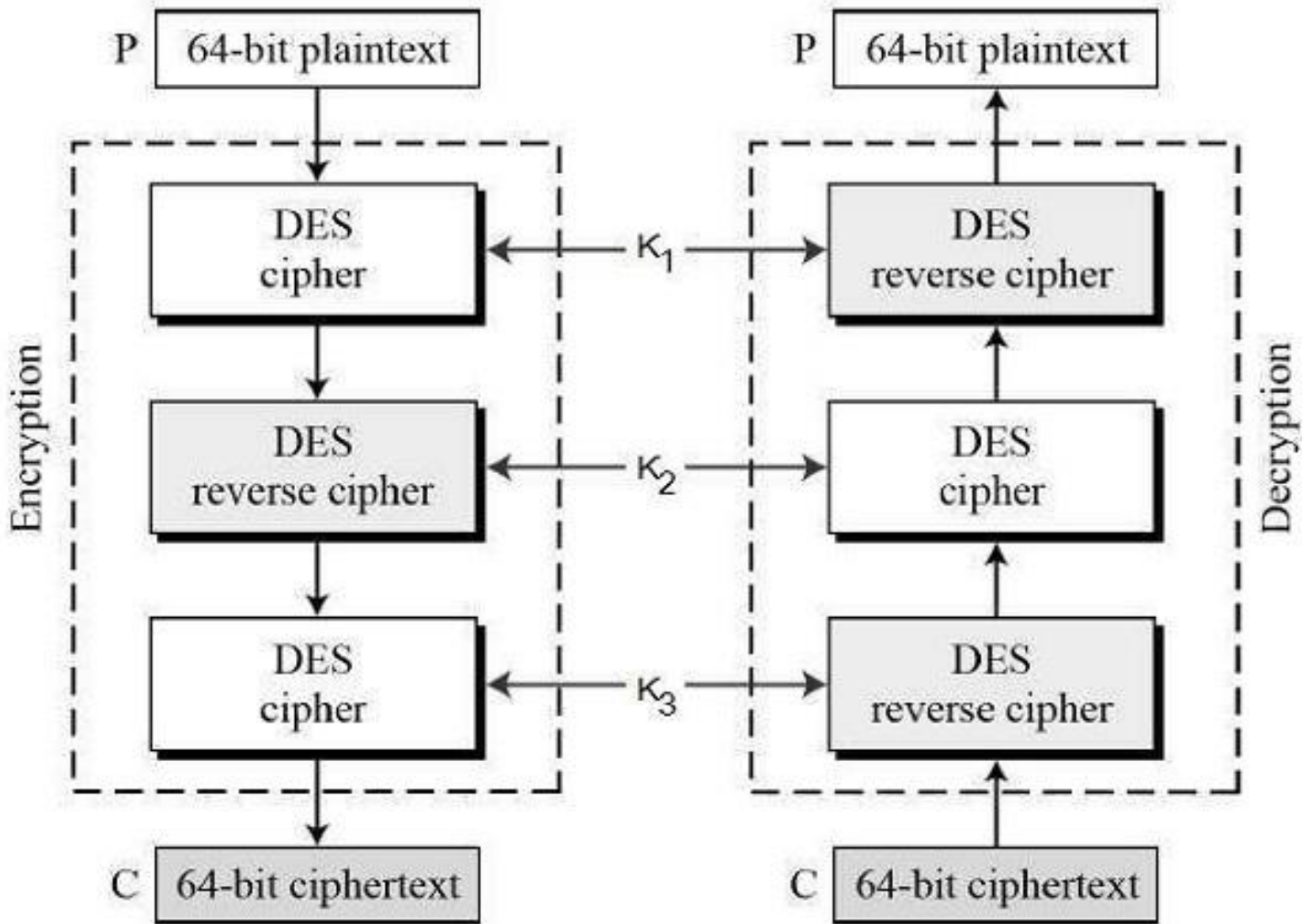


Single Round of DES Algorithm

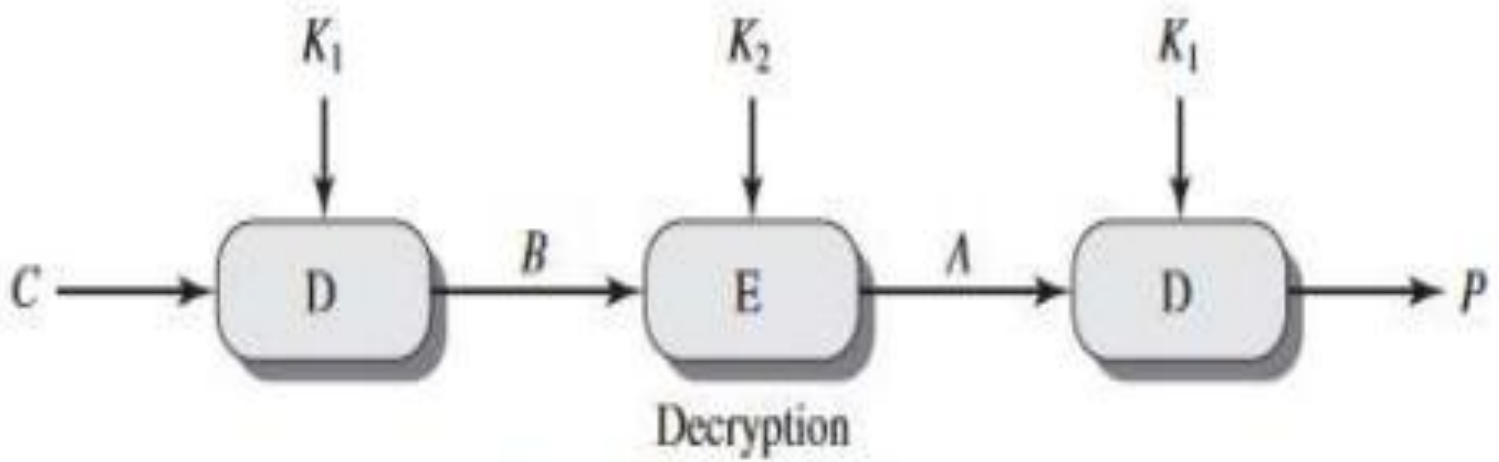
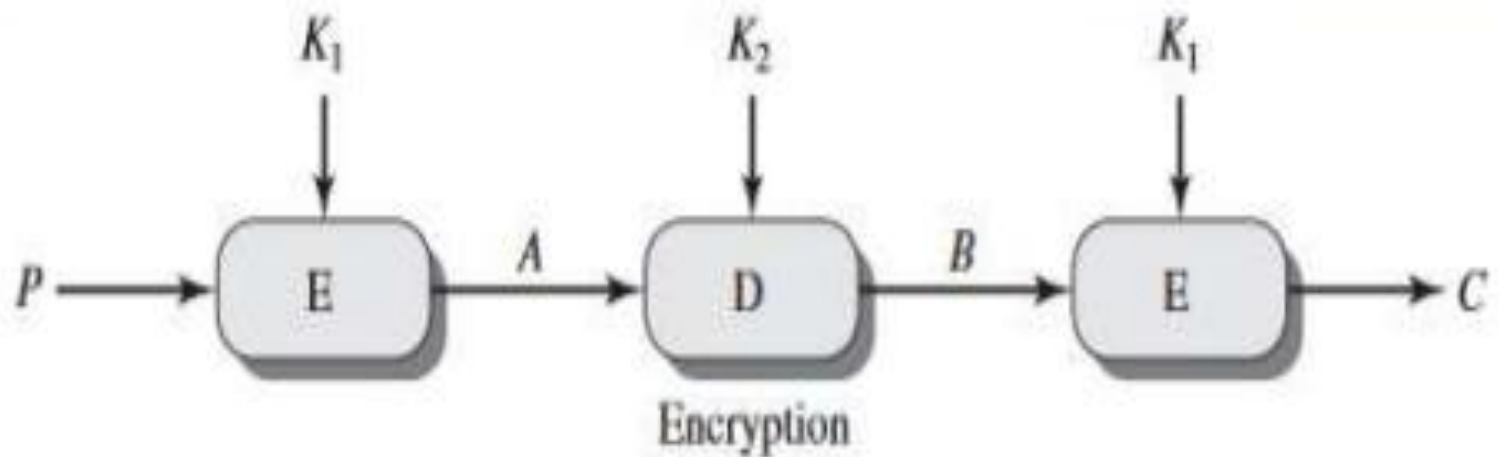
Half Block (32 bits)

Subkey (48 bits)

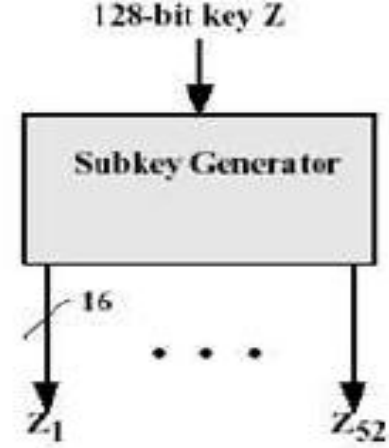
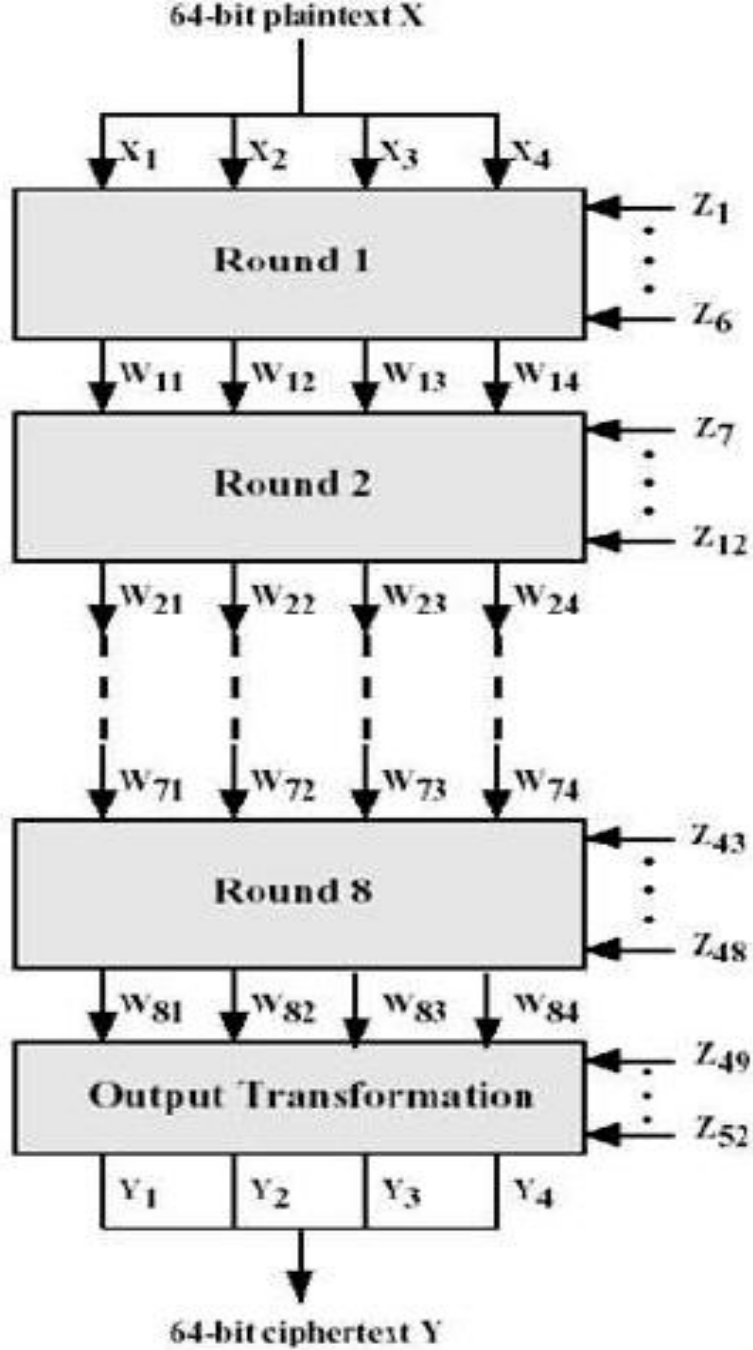




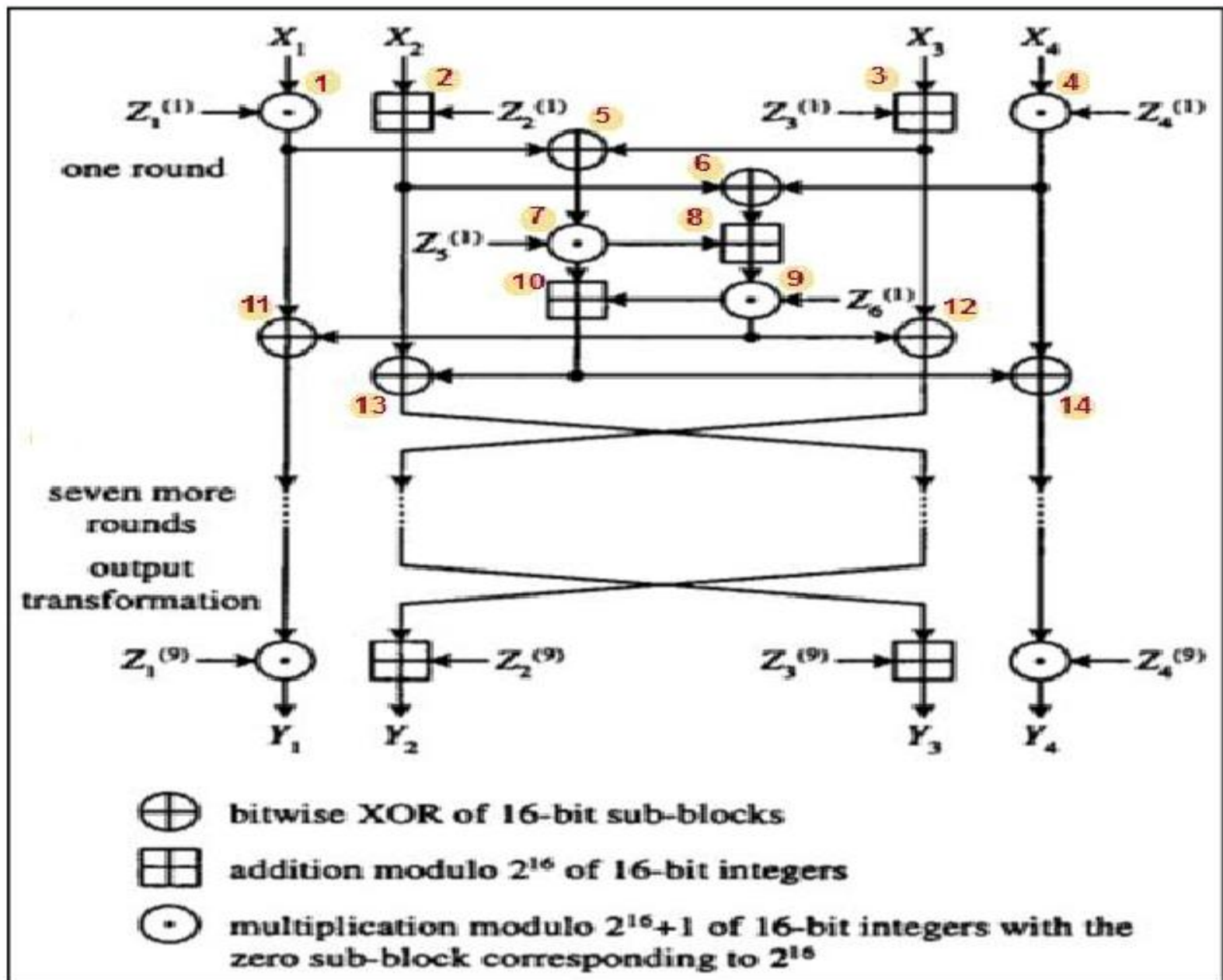
# Triple DES



**(b) Triple encryption**



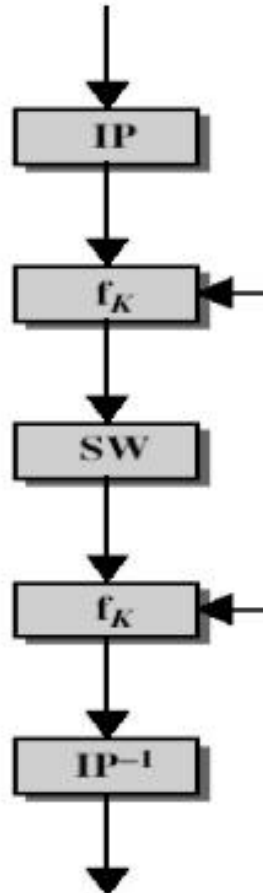
# IDEA BLOCK DIAGRAM



**Figure 2:** Structure of IDEA encryption process [3]

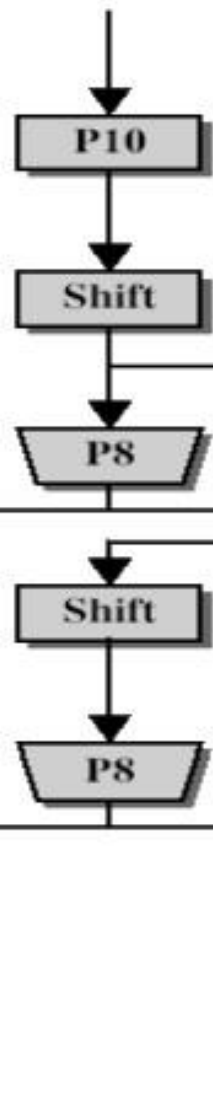
ENCRYPTION

8-bit plaintext



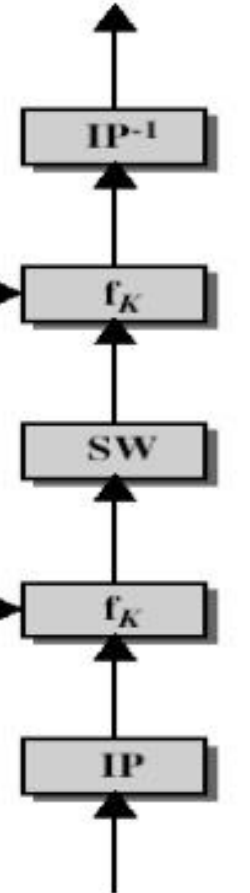
8-bit ciphertext

10-bit key



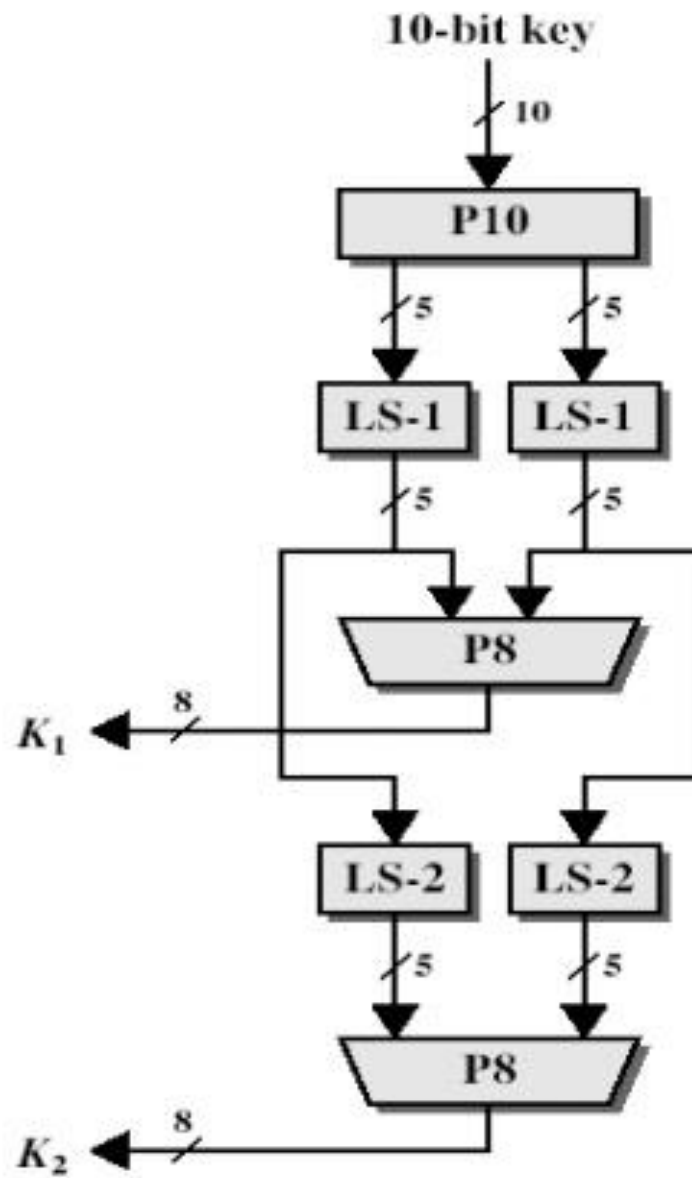
DECRYPTION

8-bit plaintext

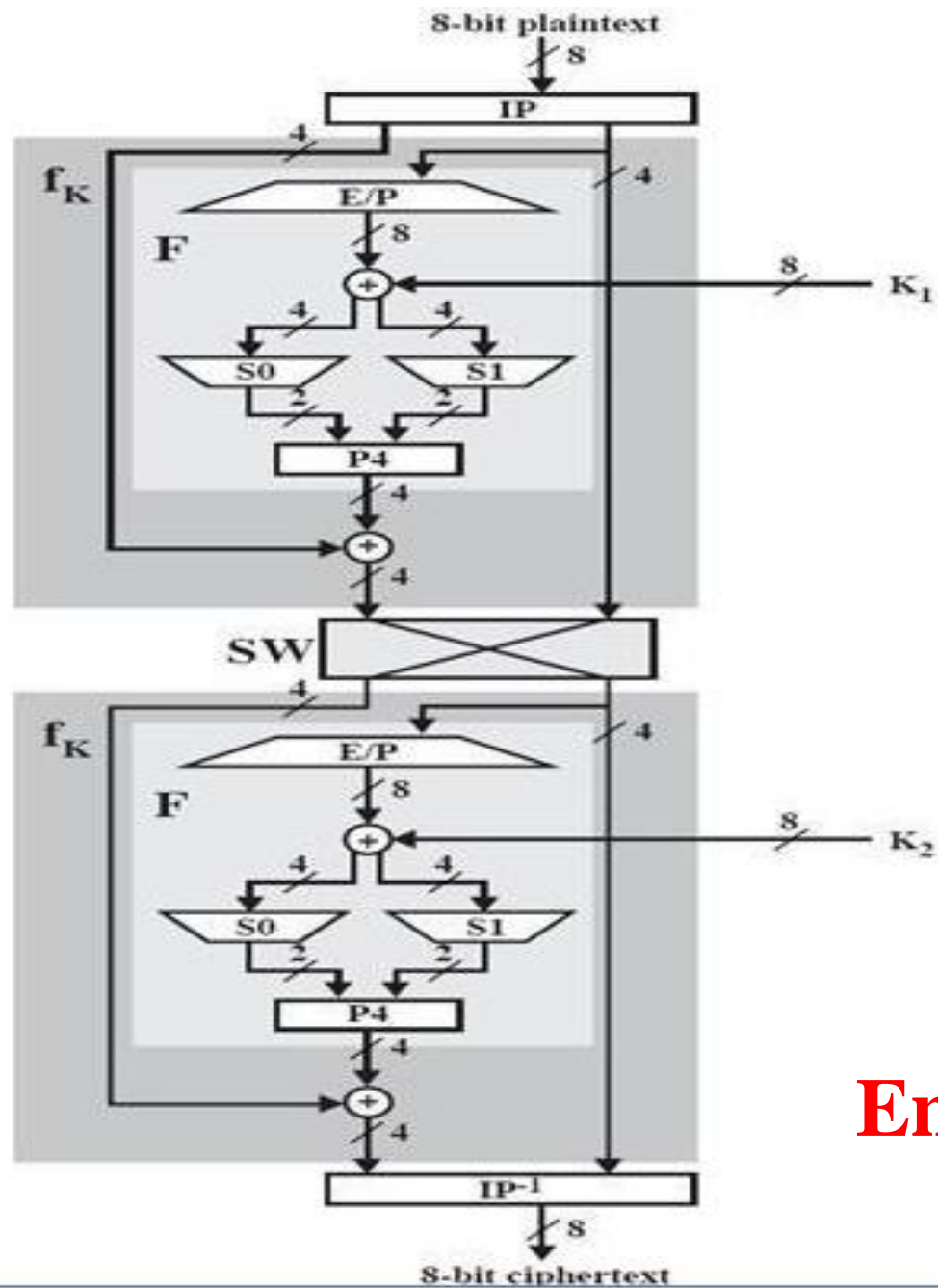


8-bit ciphertext

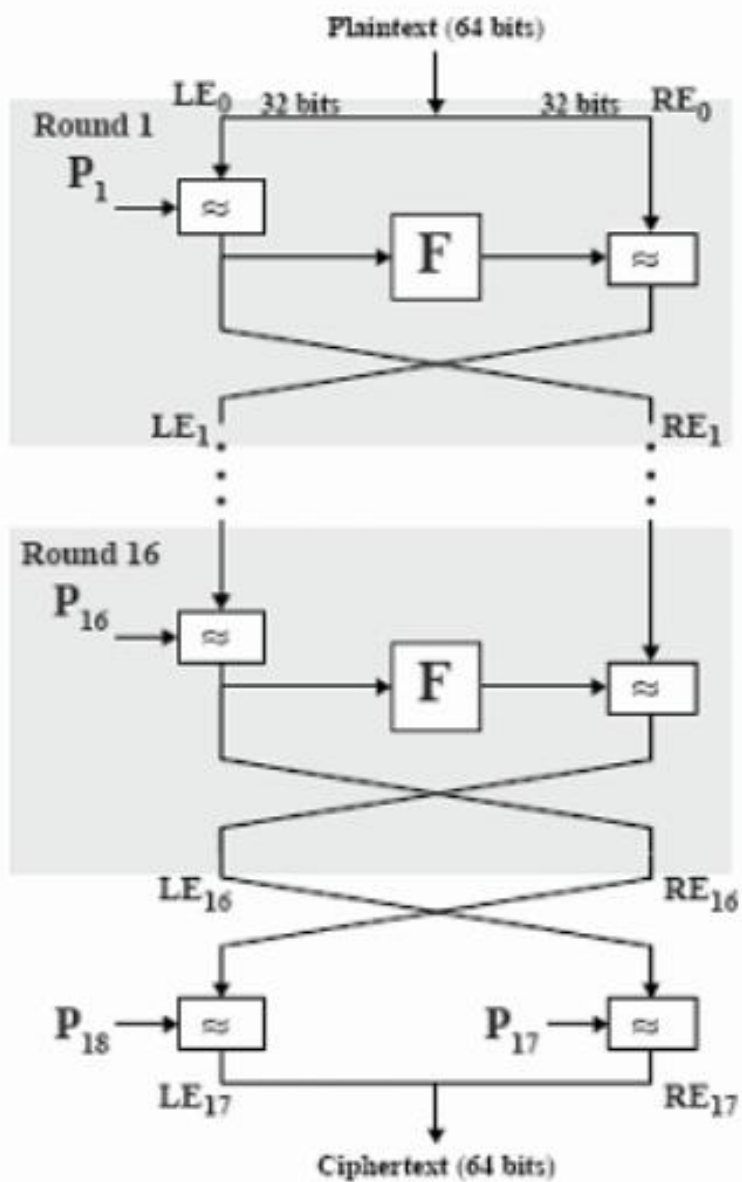
S-DES scheme



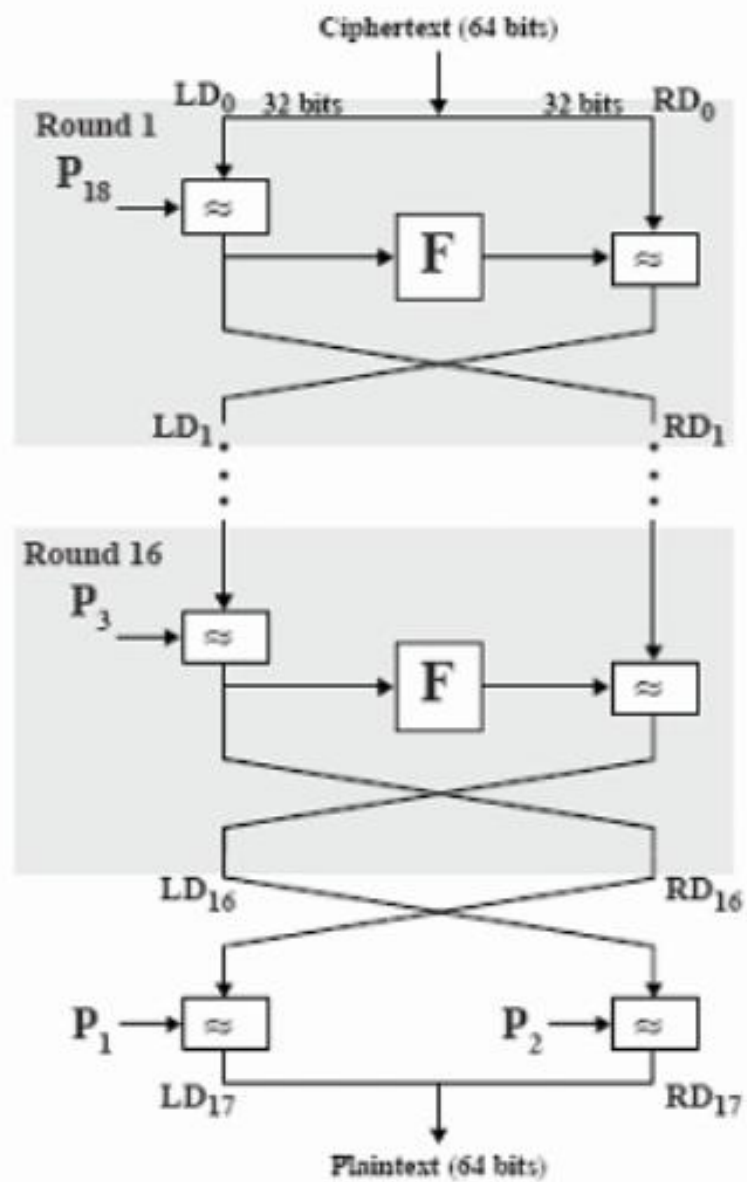
**Figure: key generation for S-DES**



## S-DES Encryption



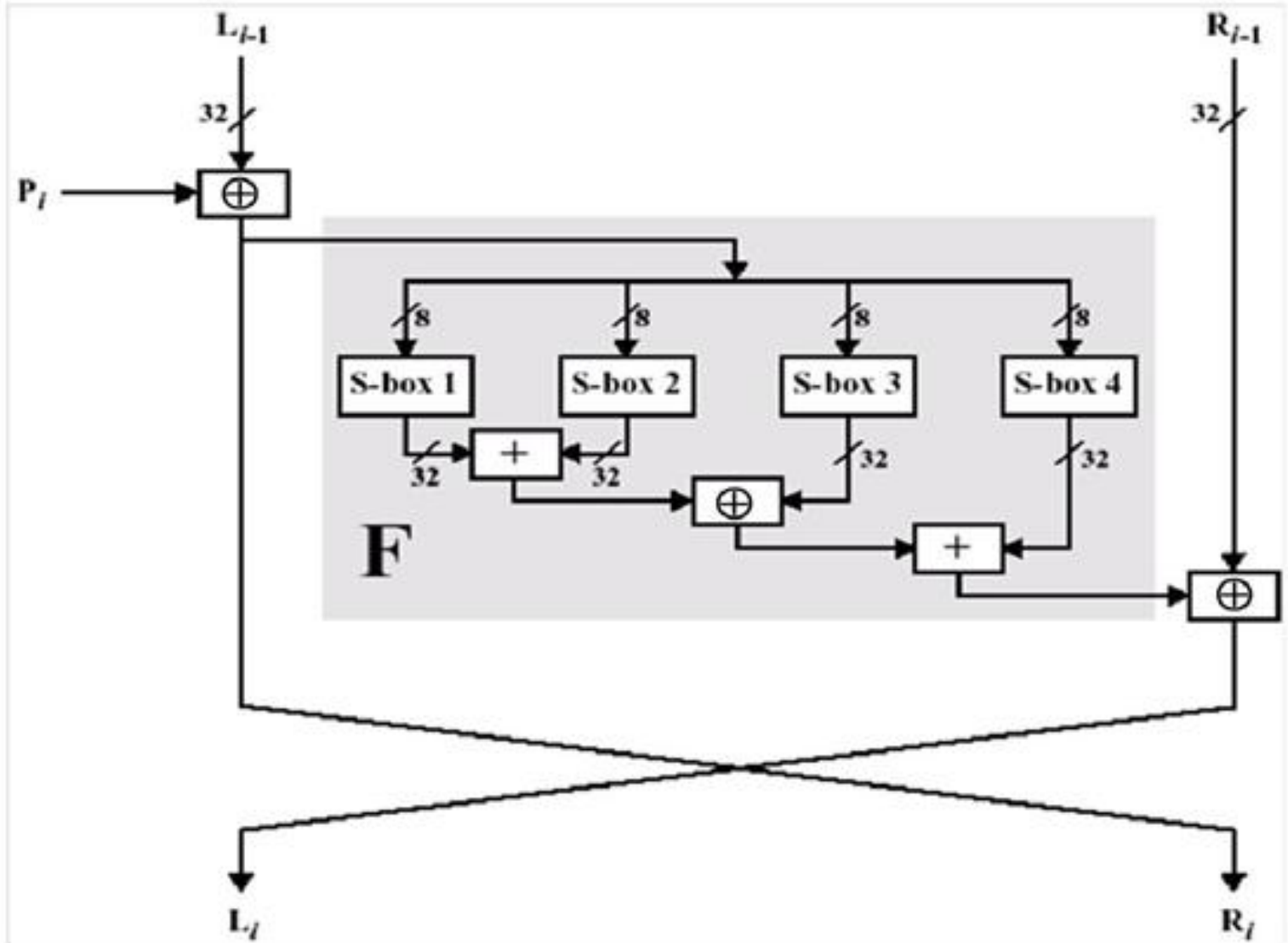
(a) Encryption



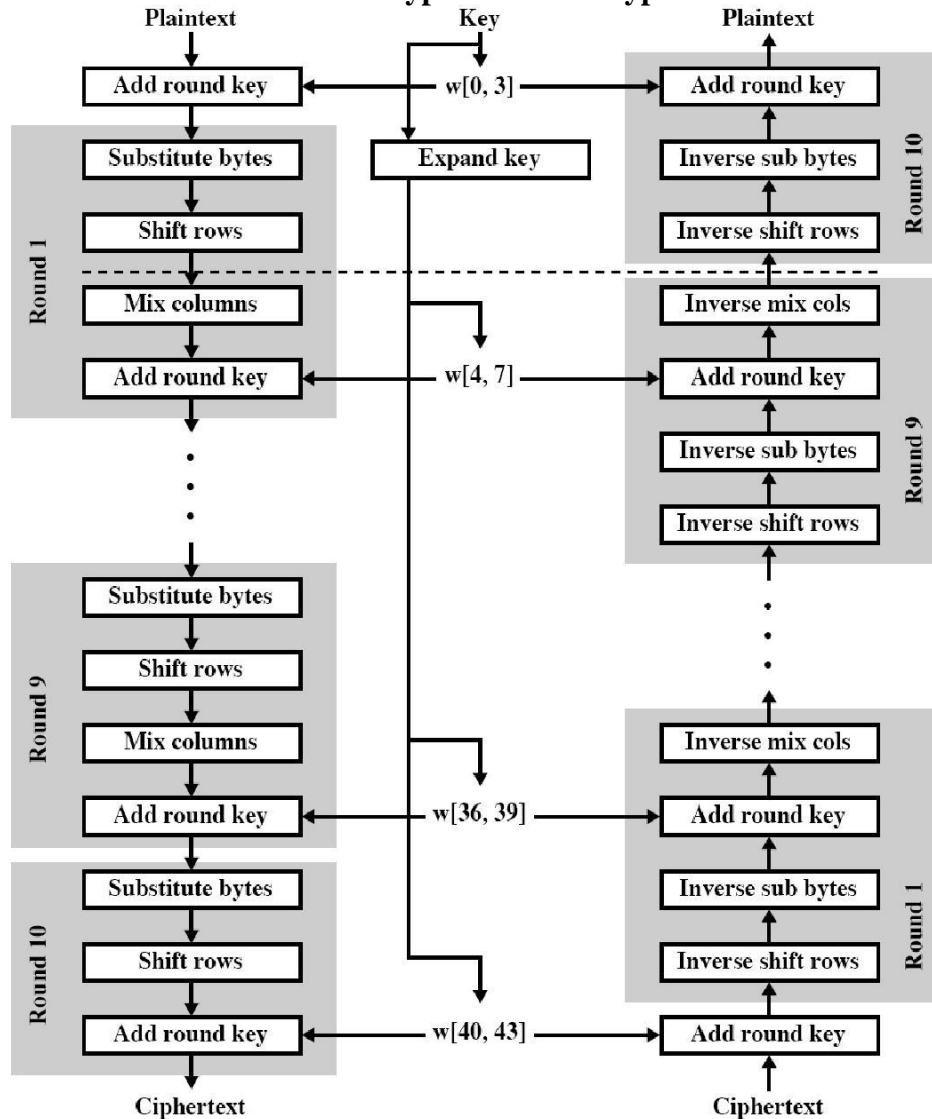
(b) Decryption

Blowfish Encryption and Decryption

# Function

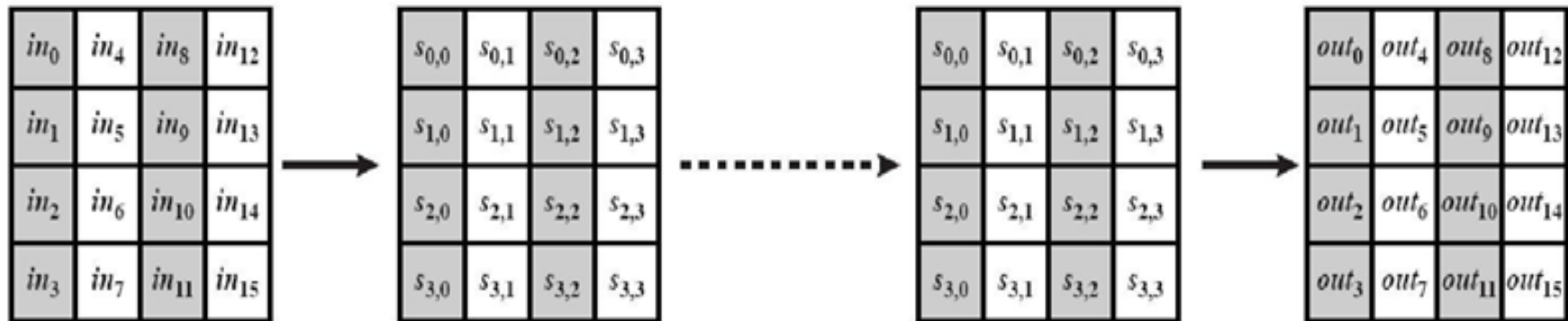


## AES Encryption and Decryption



(a) Encryption

(b) Decryption

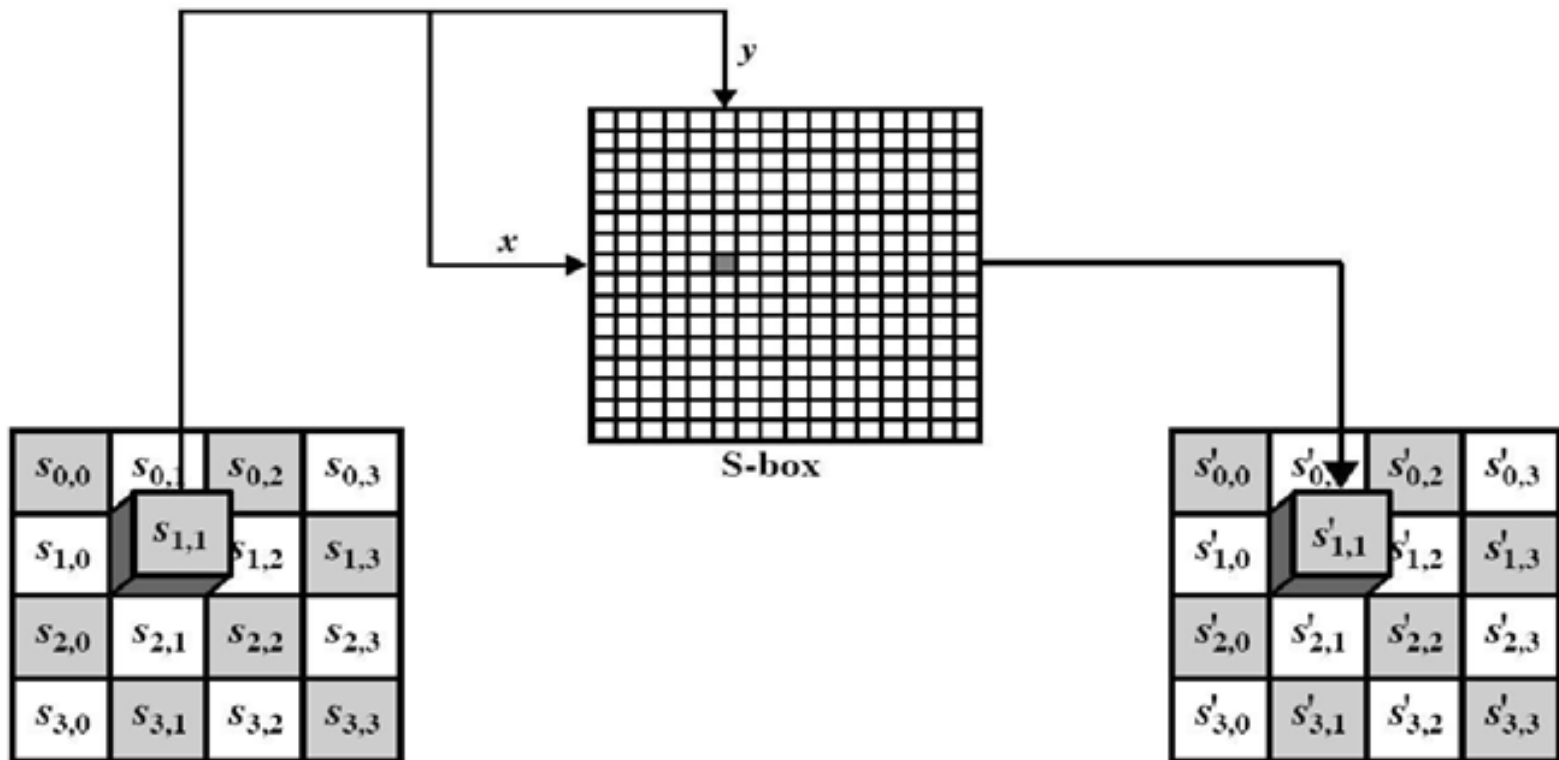


(a) Input, state array, and output



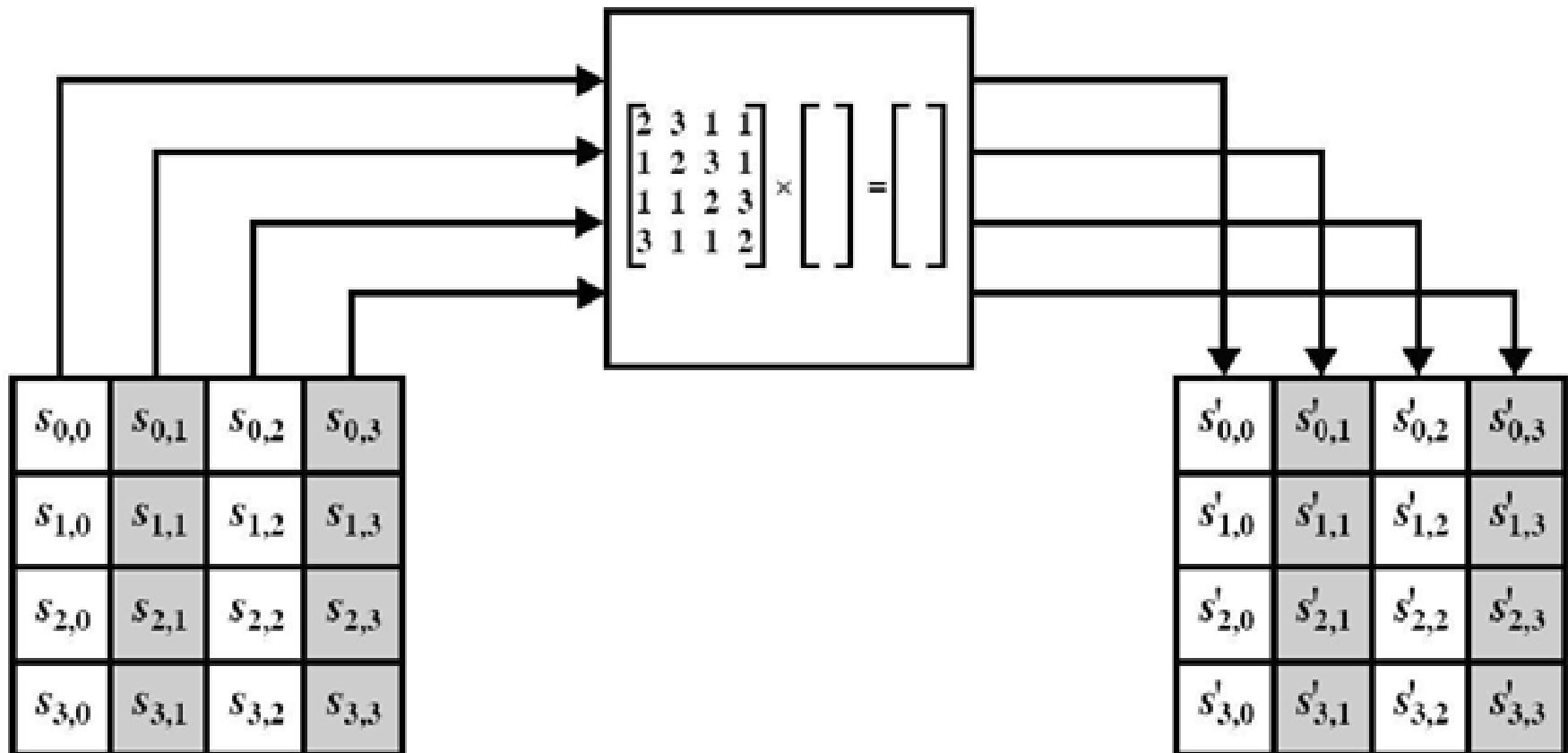
(b) Key and expanded key

# Substitute Bytes Transformation

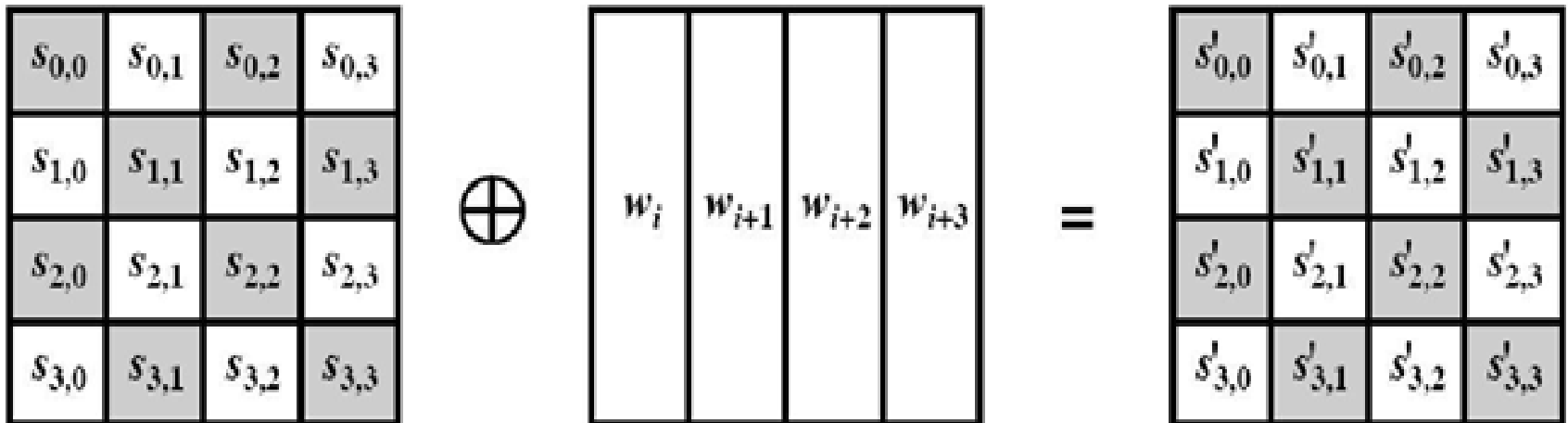




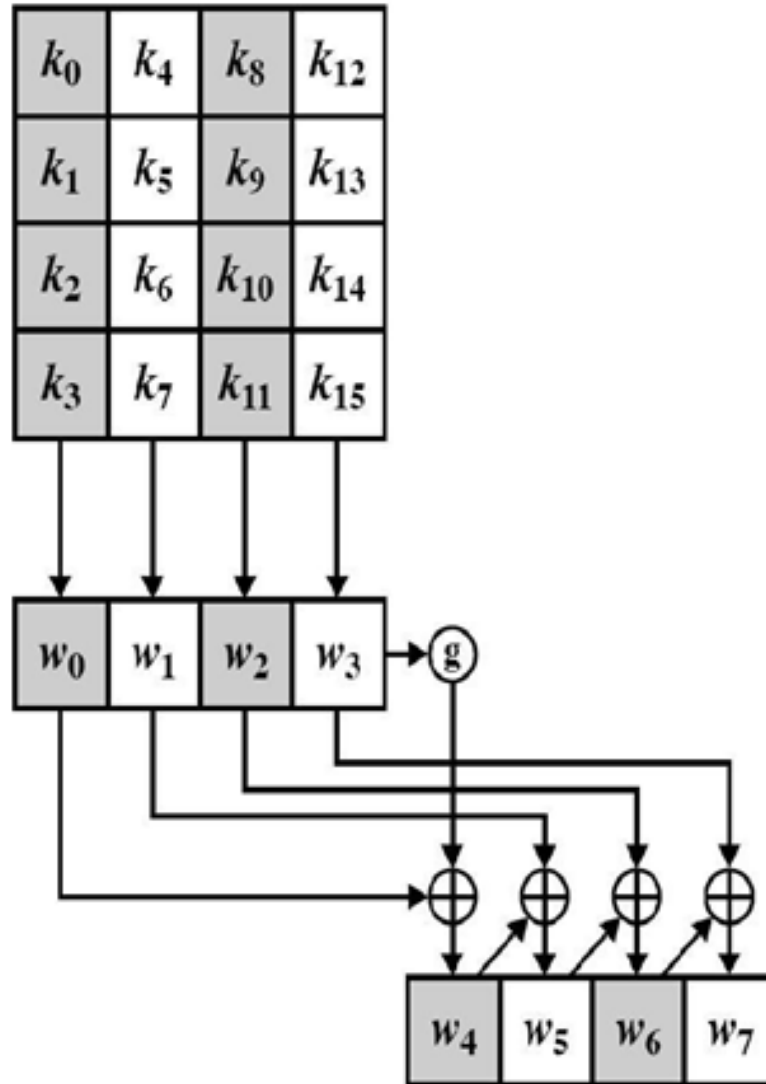
# MixColumns Transformation



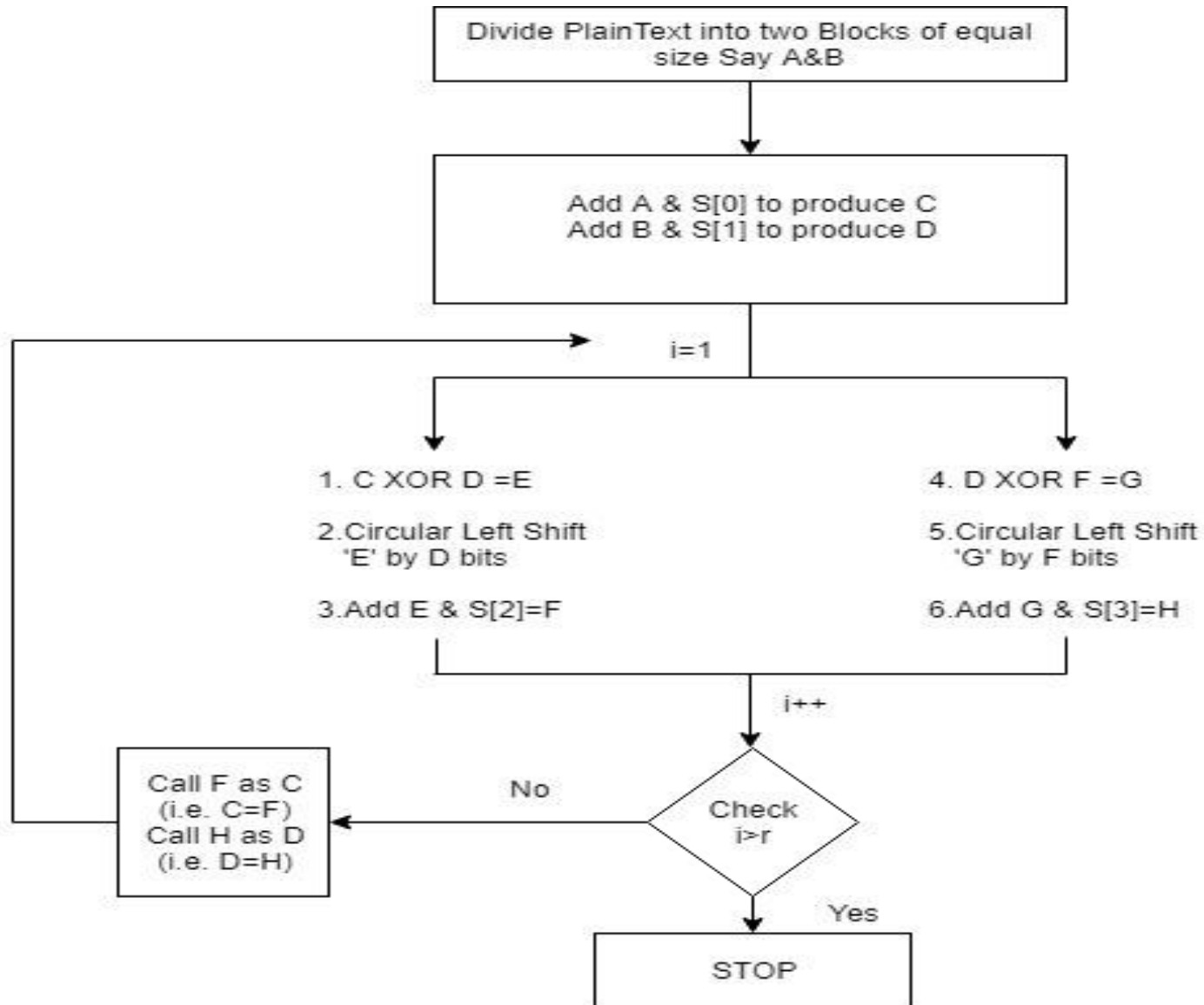
# AddRoundKey Transformation



# AES Key Expansion



# RC-5 Algorithm



We divide the plaintext block into two equal parts A and B

Then they are XOR with two subkeys  $S\{0\}$  and  $S\{1\}$

$$C = A + S[0]$$

$$D = B + S[1]$$

for  $i = 1$  to  $r$  do:

1.  $C \oplus D = E$

2. perform circular left shift on E by D bits

3. add E and  $S[2 * i]$  and store the result in F which is input for step 4

4.  $D \oplus F = G$

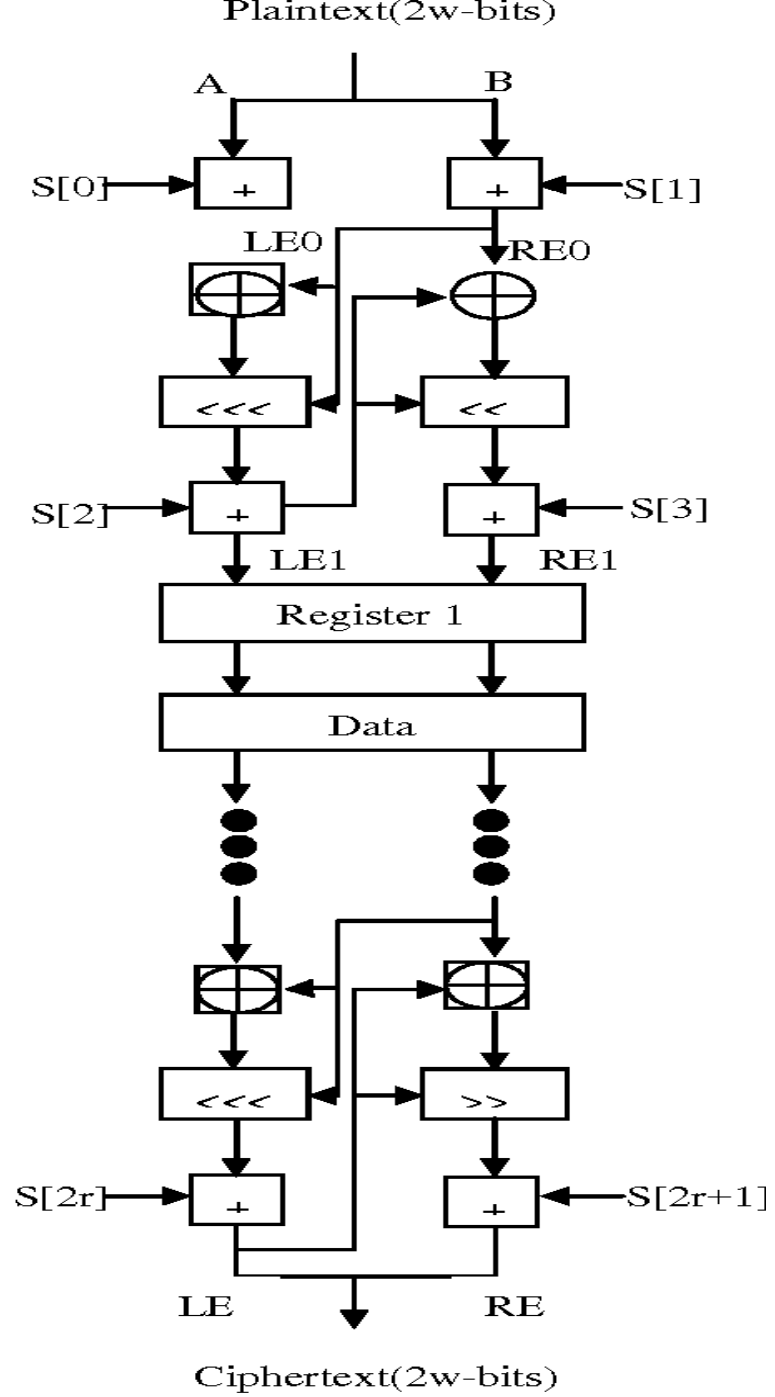
5. perform circular left shift on G by F bits

6. add G and  $S[2 * i + 1]$  and store the result in H

7. If  $i < r$

Call F as C and H as D and repeat the steps from 1 to 7

else stop



# RC4 Algorithm

## Key Scheduling:

```
j = 0;
for i = 0 to 255 do
{
    j = (j + S[i] + T[i]) mod 256;
    Swap(S[i], S[j]);
}
```

## Stream Generation:

- $i, j = 0;$
- while (true)
- $i = (i + 1) \bmod 256;$
- $j = (j + S[i]) \bmod 256;$
- $\text{Swap}(S[i], S[j]);$
- $t = (S[i] + S[j]) \bmod 256;$
- $k = S[t];$

# RSA ALGORITHM

- Choose two large prime numbers ( $p$  and  $q$ )
- Calculate  $n = p * q$  and  $\Phi n = (p-1)(q-1)$
- Choose a number  $e$  where  $1 < e < \Phi n$
- Calculate  $d = e^{-1} \text{mod } \Phi n$
- You can bundle private key pair as  $(n, d)$
- You can bundle public key pair as  $(n, e)$

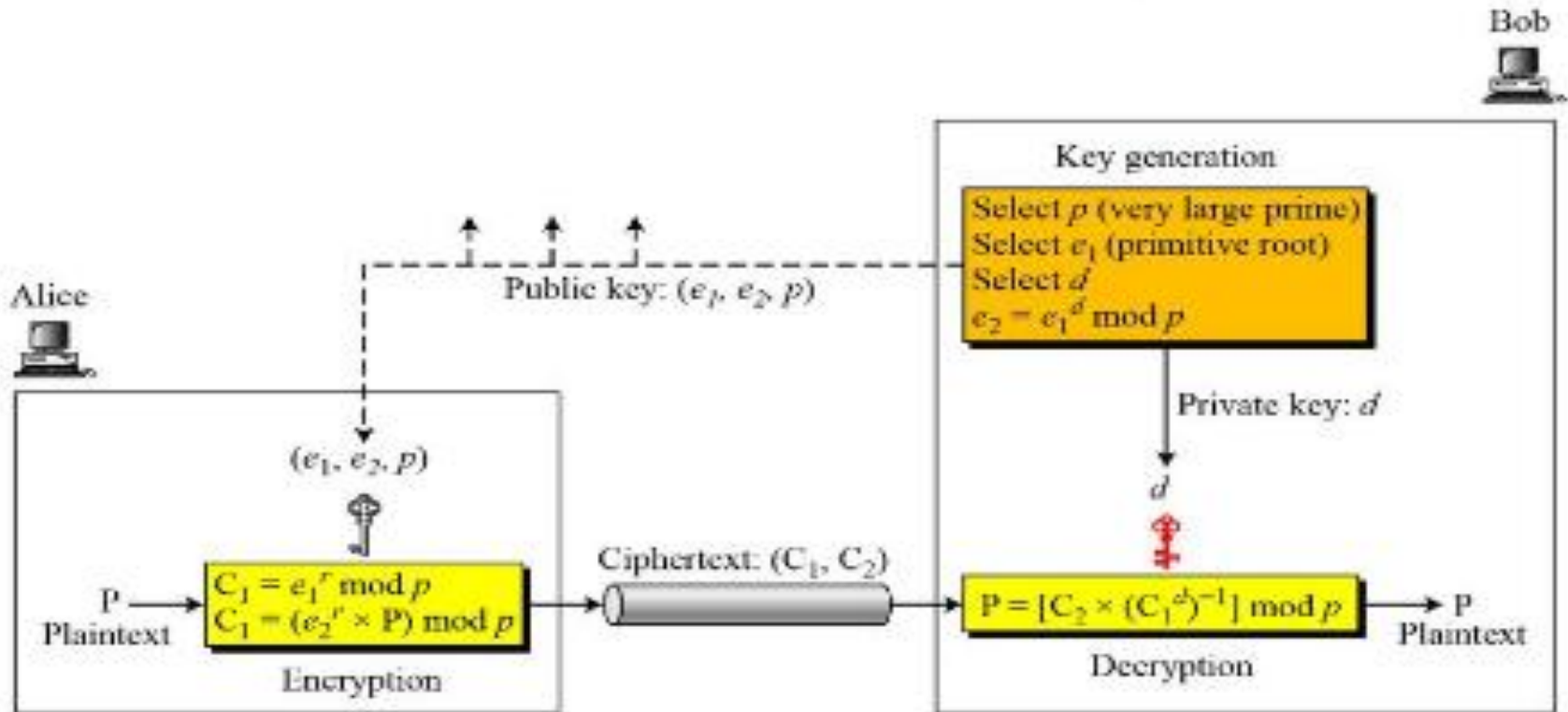
## Encryption/Decryption Function

- If the plaintext is  $m$ , ciphertext =  $m^e \text{ mod } n$ .
- If the ciphertext is  $c$ , plaintext =  $c^d \text{ mod } n$

# Elgamal cryptography

El gamal cryptography works in 3 steps/stages

- Key generation
- Elgamal encryption
- Elgamal decryption



# Elgamal cryptography Algorithm

## A. Elgamal key generation:

- Select a large prime number 'p'
- Select encryption key 'e'1' to be primitive root of mod p
- Select decryption key 'd' such that  $1 \leq d \leq p-2$
- Calculate encryption key 'e'2' such that
- $e2 = e1^d \text{ mod } p$
- Form the set i,e public key (e1,e2,p) to be announced publicly
- Private Key 'd' to be kept secret.

## B. Elgamal key encryption:

- Select a random number 'r'
- Compute the first part of ciphertext 'c'1,  $c1 = e1^r \text{ mod } p$
- Compute the second part of ciphertext 'c'2,  $c2 = (e2^r * PT) \text{ mod } p$

## C. Elgamal key decryption:

- Calculate the PT
- $PT = (c2 * (c1^d)^{-1}) \text{ mod } p$

# DIFFIE-HELLMAN KEY EXCHANGE

## Global Public Elements

$q$	prime number
$\alpha$	$\alpha < q$ and $\alpha$ a primitive root of $q$

## User A Key Generation

Select private $X_A$	$X_A < q$
Calculate public $Y_A$	$Y_A = \alpha^{X_A} \bmod q$

## User B Key Generation

Select private $X_B$	$X_B < q$
Calculate public $Y_B$	$Y_B = \alpha^{X_B} \bmod q$

## Generation of Secret Key by User A

$$K = (Y_B)^{X_A} \bmod q$$

## Generation of Secret Key by User B

$$K = (Y_A)^{X_B} \bmod q$$

# KNAPSACK ALGORITHM

## Example –

- $\{1, 2, 4, 10, 20, 40\}$  is a super increasing as
- $1 < 2$ ,  $1+2 < 4$ ,  $1+2+4 < 10$ ,  $1+2+4+10 < 20$  and  $1+2+4+10+20 < 40$ .

## Derive the Public key

- **Step-1:**  
Choose a super increasing knapsack  $\{1, 2, 4, 10, 20, 40\}$  as the private key.
- **Step-2:**  
Choose two numbers  $n$  and  $m$ . Multiply all the values of private key by the number  $n$  and then find modulo  $m$ . The value of  $m$  must be greater than the sum of all values in private key, for example 110. And the number  $n$  should have no common factor with  $m$ , for example 31.
- **Step-3:**  
Calculate the values of Public key using  $m$  and  $n$ .
  - $1 \times 31 \bmod(110) = 31$
  - $2 \times 31 \bmod(110) = 62$
  - $4 \times 31 \bmod(110) = 14$
  - $10 \times 31 \bmod(110) = 90$
  - $20 \times 31 \bmod(110) = 70$
  - $40 \times 31 \bmod(110) = 30$
- Thus, our public key is  $\{31, 62, 14, 90, 70, 30\}$   
And Private key is  $\{1, 2, 4, 10, 20, 40\}$ .

Now take an example for understanding the process of encryption and decryption.

### Example –

Lets our plain text is **100100111100101110**.

#### 1. Encryption :

As our knapsacks contain six values, so we will split our plain text in a groups of six:

- **100100 111100 101110**

Multiply each values of public key with the corresponding values of each group and take their sum.

- **100100 {31, 62, 14, 90, 70, 30}**
- **$1 \times 31 + 0 \times 62 + 0 \times 14 + 1 \times 90 + 0 \times 70 + 0 \times 30 = 121$**
  
- **111100 {31, 62, 14, 90, 70, 30}**
- **$1 \times 31 + 1 \times 62 + 1 \times 14 + 1 \times 90 + 0 \times 70 + 0 \times 30 = 197$**
  
- **101110 {31, 62, 14, 90, 70, 30}**
- **$1 \times 31 + 0 \times 62 + 1 \times 14 + 1 \times 90 + 1 \times 70 + 0 \times 30 = 205$**
- **So, our cipher text is 121 197 205.**

## 2. Decryption :

The receiver receive the cipher text which has to be decrypt. The receiver also knows the values of  $m$  and  $n$ .

So, first we need to find the  $x$ , which is multiplicative inverse of  $n \bmod m$  i.e.,

- $n \times x \bmod(m) = 1$
- $31 \times x \bmod(110) = 1 \Rightarrow x = 71$

Now, we have to multiply 71 with each block of cipher text take modulo  $m$ .

- $121 \times 71 \bmod(110) = 11$

Then, we will have to make the sum of 11 from the values of private key  $\{1, 2, 4, 10, 20, 40\}$  i.e.,

$$1+10=11$$

so make that corresponding bits 1 and others 0 which is **100100**.

Similarly,

- $197 \times 71 \bmod(110) = 17$
- $1+2+4+10=17 = 111100$

- And,  $205 \times 71 \bmod(110) = 35$

- $1+4+10+20=35 = 101110$

- After combining them we get the decoded text. **100100111100101110** which is our plain text.